

Module 1: Types and Expressions

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for comments that improved these slides

Prepared for 2u

Semester Online

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1.0 Introduction

- **What is a *type*?**
 - A classification of items in the world based on
 - The kinds of things an item can do
 - The
 - integers, real numbers, character strings,
- **As types, consider integers and real numbers**
 - integer
 - Useful for counting
 - Number of playing cards in a deck
 - Real number
 - Can include fractional values
 - Temperature readings and averages, interest rates
 - On the computer, we can only approximate real numbers
- **Data types in computer science**
 - Represent values of interest
 - Allow operations that make sense
- **Built in data types (in this module)**
 - For representing integers, interest rates, names, addresses, facts
- **Later, we design our own types**
 - Bank account, hockey player, song
- **The best choice of data type is not always obvious**
 - Should you use an integer or a real number?
 - You might start with one, and change your mind later
 - Height – might be integer number of centimeters
 - But if we're measuring something small, fractional values may be needed
- **There are rarely right or wrong choices**
 - But a choice will have its advantages and disadvantages
 - Picking a suitable data type is an engineering process and is based on currently understood constraints and best planning for the future. The future can at times seem uncertain.
 - Example: Y2K

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 - How many exams will be given?
 - How many words are in this sentence?

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 - How many exams will be given?
 - How many words are in this sentence?
- The above are 0 or positive, but negative values may be of interest as well
 - How many days until your 21st birthday?
 - The week before, 7
 - The week after, -7
 - How has the class size changed since yesterday?
 - +5 students were added
 - -3 students dropped

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- For example, Java's `int` type:
 - Minimum value: `-2,147,483,648`
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 - But how about the distance from Earth to Sun?

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 - But how about the distance from Earth to Sun?
 - In meters: `149,597,870,700` Too big!
 - We can represent values outside of the range of an `int` using techniques we learn later.
 - For now, we consider an `int` sufficient.

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 - We can represent values outside of the range of an `int` using techniques we learn later.
 - For now, we consider an `int` sufficient.
- There are things we cannot represent conveniently with an `int`
 - Your name (need the alphabet, not just 0—9)
 - Your height in meters (need fractions)
 - Whether you are vegetarian or not
- We will see other data types soon that help us with those

1.1 Our first data type: int

- How do we represent a concept using the `int` data type? We do this by specifying:
 - The type of the concept (`int`)
 - A name for the concept (`numStudents`, `numExams`, etc.)
 - A value for the concept
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```
int numStudents = 390;
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 - Each subsequent word begins with an upper-case letter
 - There are no spaces (blanks) in a variable name
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- The name should be meaningful, clear, and relevant to the concept

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- Any valid expression can appear on the right-hand side

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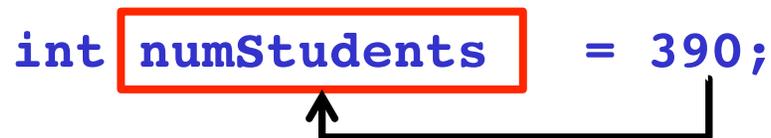
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- An assignment statement is evaluated as follows
 - The value of the right-hand side is computed (390 in this case)

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- An assignment statement is evaluated as follows
 - The value of the right-hand side is computed (390 in this case)
 - The result is stored at the name declared on the left-hand side

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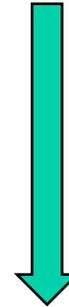
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int numWaitListed = 20;
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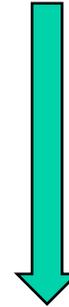
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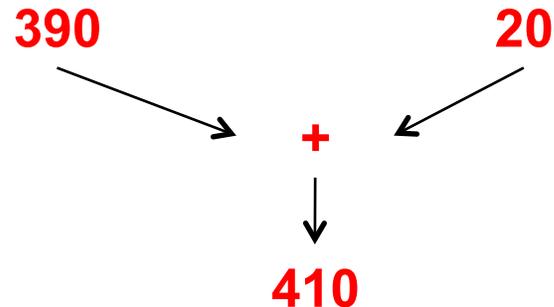
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```
int totalStudents = numStudents + numWaitListed;
```



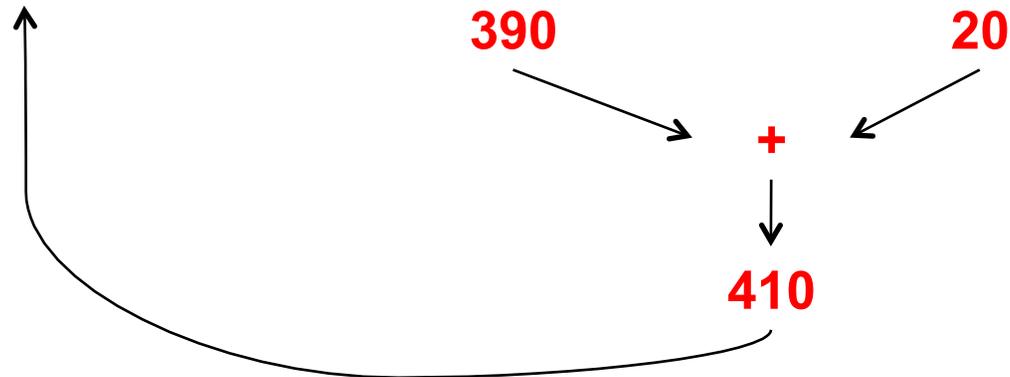
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- **The computer executes your statements in sequence**

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Variable Name	Value
numStudents	390
numWaitListed	20
totalStudents	410

```
int numStudents = 390;
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```
int totalStudents = numStudents + numWaitListed;
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    numStudents = numStudents + 5;
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Because we are assigning a previously-declared variable `numStudents` a new value, its type has already been declared as `int`, and we are not allowed to declare its type ever again

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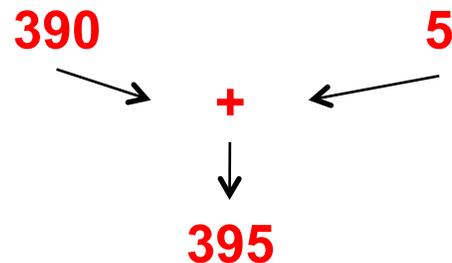
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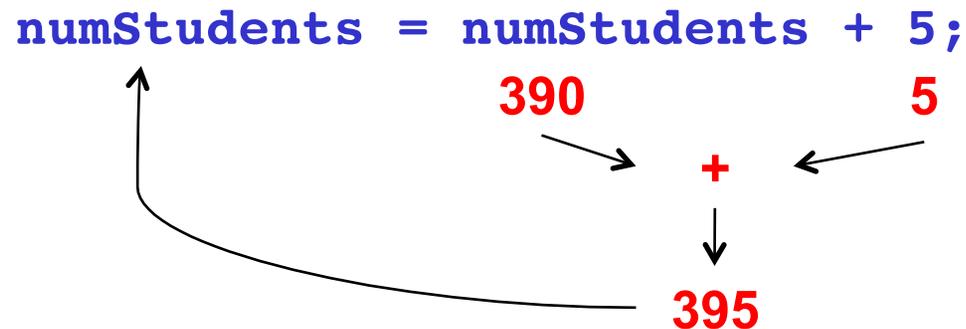
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int numStudents = 390;
```

```
int numWaitListed = 20;
```

```
int totalStudents = numStudents + numWaitListed;
```

```
  numStudents = numStudents + 5;
```

- Remember: we do *not* re-declare numStudents
 - It is already known to be an int
 - The new value simply replaces the old value

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- The computer executes your statements in sequence

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```
int totalStudents = numStudents + numWaitListed;
```

```
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```

- Other values are *not* automatically updated
 - They have only been assigned their initial value
 - Code executes from the top, reading down

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Variable Name	Value
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totalStudents	415

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int numWaitListed = 20;
```

```
int totalStudents = numStudents + numWaitListed;
```

```
    numStudents = numStudents + 5;
```

```
totalStudents = numStudents + numWaitListed;
```

1.1b Exercise

- **Video intro**
 - **Important to try things out in small doses**
 - **Story**
 - Alice has 7 carrots
 - Bob has 3 more than Alice
 - Charles has 4 times as many as Alice
 - Also, Charles stole all of Bob's carrots
 - Diane has twice as many as Charles
- **Question card: Translate the story to code**
 - **Print out how many Diane has at the end**
 - `System.out.println(dianeCarrots);`
- **Response: go over my solution**

Roundtable 1.1c Now get input from the user

- **Student asks question about how to make Alice's carrots a value input by the user**
 - Much more on this later
 - But for now we use the `ArgsProcessor` stuff
- **Show what happens when we try to use it**
 - import the right thing with eclipse's help
- **Meaningful prompting messages**
- **Run it a few times**

1.2 Operations on `int` types

- **Most operations work as expected**
 - **+ plus**
 - **- minus**
 - *** times**
- **One operation usually surprises students and experienced programmers alike**
 - **Division using the / operator**
 - **Returns an `int`, so no fractional values are allowed**
 - **The value returned is as if the digits past the decimal point were dropped**

Expression	Value
<code>4 / 2</code>	<code>2</code>

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Expression	Value
4 / 2	2
3 / 2	1
5 / 2	2

1.2 Operations on `int` types

- Most operations work as expected
 - + plus
 - - minus
 - * times
- One operation usually surprises students and experienced programmers alike
 - Division using the / operator
 - Returns an `int`, so no fractional values are allowed
 - The value returned is as if the digits past the decimal point were dropped
 - We are not allowed to divide by 0

Expression	Value
4 / 2	2
3 / 2	1
5 / 2	2
7 / 0	Error !

1.2 Operations on `int` types

- The `%` operator computes the remainder after division

<code>x</code>	<code>y</code>	<code>x / y</code>	<code>x % y</code>
4	2	2	0

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- The `%` operator computes the remainder after division

<code>x</code>	<code>y</code>	<code>x / y</code>	<code>x % y</code>
4	2	2	0
3	2	1	1
5	2	2	1

Why is this useful?

1.2 Operations on `int` types

- The `%` operator computes the remainder after division
- Examples:
 - Convert a large number of pennies into dollars and cents

```
int pennies = 789321;
```

Variable Name	Value
pennies	789321

1.2 Operations on `int` types

- The `%` operator computes the remainder after division
- Examples:
 - Convert a large number of pennies into dollars and cents

```
int pennies = 789321;
```

```
int dollars = pennies / 100;
```

Variable Name	Value
pennies	789321
dollars	7893

1.2 Operations on int types

- The % operator computes the remainder after division
- Examples:
 - Convert a large number of pennies into dollars and cents

```
int pennies = 789321;
```

```
int dollars = pennies / 100;
```

```
int cents = pennies % 100;
```

Variable Name	Value
pennies	789321
dollars	7893
cents	21

1.3 Exercise

- **Video intro**
 - We see how to take a number of pennies and compute the dollars and cents contained therein
 - First we'll write code for that much and make sure it works.
 - Then we will incrementally improve the code
 - Allow quarters in change
 - Allow nickels and dimes too

1.3 Exercise

- **Question card**
 - **Write code that gives change as follows:**
 - Prompt the user for a number of pennies
 - Call this value `initialPennies`
 - Compute `d` as the number of dollars contained therein
 - Let's assume the user trades in the appropriate number of pennies for the `d` dollars
 - Compute `penniesLeftAfterDollars` as the number of pennies that remain
 - Print out the dollars and cents that are contained in the `initialPennies`
 - **Try out your code and make sure that it works**

1.3 Exercise

- **Question card**
 - **Now improve your code so that quarters can be given as well**
 - Assume `penniesLeftAfterDollars` remain after dollars are given
 - How many quarters could be substituted for that many pennies? Call this value `q` and print it out as well as the pennies left over after dollars and quarters are exchanged
- **Example: 798 pennies**
 - **7 dollars, leaving 98 penniesAfterCollars**
 - **q=3 quarters in 98 pennies**
 - **23 pennies left over**

1.3 Exercise

- **Question card**
 - **Now improve your code so that change can be made**
 - dollars
 - quarters
 - dimes
 - nickels
 - pennies left over

1.3 Exercise

- **Example**

- **798 pennies initially**

- **Should get**

- 7 dollars, leaving 98 cents

- 3 quarters, leaving $98 - 75 = 98 \% 25 = 23$ cents

- 2 dimes, leaving 3 cents

- 0 nickels

- 3 pennies

1.3 Exercise

- **Video response**

- Goes over a correct solution line by line using the example from the setup
- How would we verify that the answer we produced was correct?

- $d*100 + q*25 + d*10 + n*5 + p$ should equal `initialPennies`

Roundtable

- **Conversation about implementation of math on computers**
 - **If we have the largest integer value and add 1 to it, what happens?**
 - Show this with screenflow movie
- **We see computers of all sizes**
 - **Desktops, laptops, cell phones, smart watches**
 - **The basic hardware mechanisms of those computers can perform arithmetic differently**
 - Largest and smallest values
- **Java requires all computers to perform arithmetic Java's way**
 - **Because of Internet applets**
 - **A Java program runs the same way anywhere**
 - **Widespread portability and software reliability**

1.4 Building Bigger Expressions

- **We can combine smaller expressions into bigger**
 - **Using operators between smaller expressions**
 - **Using parentheses**
 - To direct the order of evaluation
 - To improve the clarity of the expression
- **My Dear Aunt Sally**
 - **Multiplication and Division have higher precedence**
 - **Addition and Subtraction have lower precedence**
 - **Evaluation is otherwise left-to-right**
 - **Parenthesized expressions have highest precedence**

1.4 Building Bigger Expressions

Expression	Value	Notes
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$(3 + 4) * 2$	14	Parentheses affect the order

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$(3 + 4) * 2$	14	Parentheses affect the order
$4 - 3 - 2 - 1$	-2	Should you use parentheses here to make this clearer?

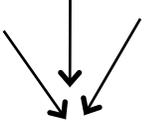
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$3 + 4 * 2$	11	$4 * 2$ computed first (MDAS)
$3 + (4 * 2)$	11	Same result as above, but clearer. The parentheses are not necessary but they make the expression easier for humans to understand
$(3 + 4) * 2$	14	Parentheses affect the order
$4 - 3 - 2 - 1$	-2	Should you use parentheses here to make this clearer?
$4 - (3 - (2 - 1))$	2	To get this result, parentheses are necessary

1.4 Building Bigger Expressions

- To understand how an expression is computed, we draw its *evaluation tree*
- Evaluation proceeds from the leaves of the tree toward its root
- A node can be computed only when the values from all of its children are available

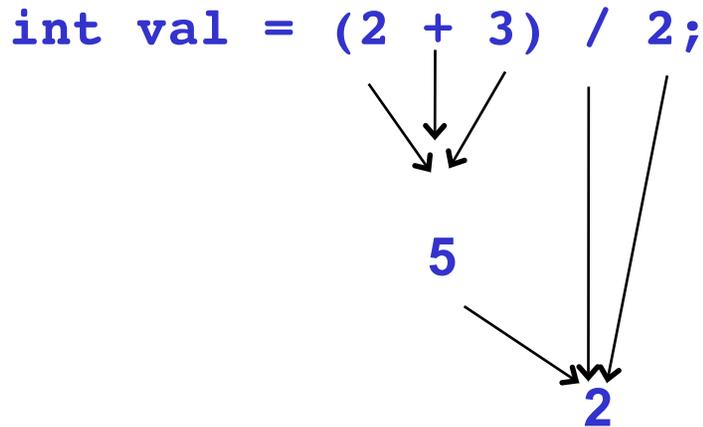
```
int val = (2 + 3) / 2;
```



5

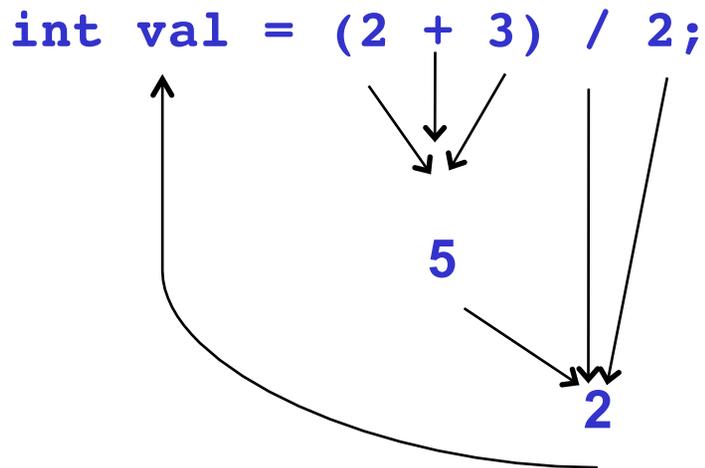
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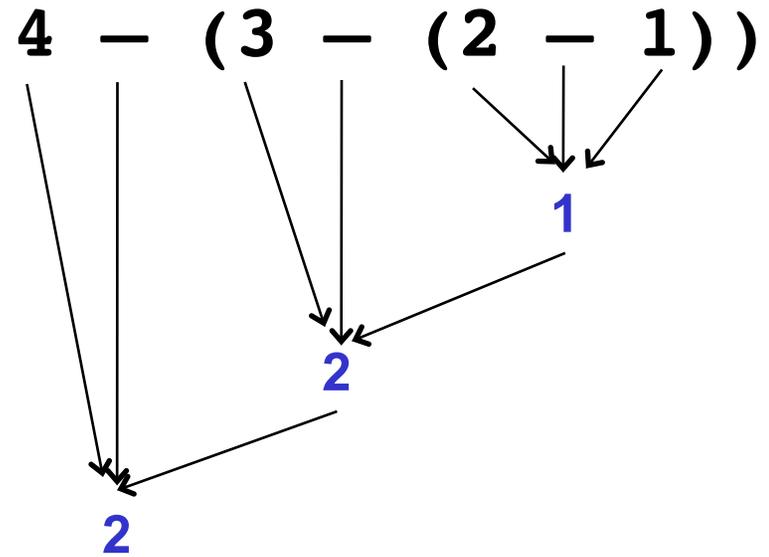
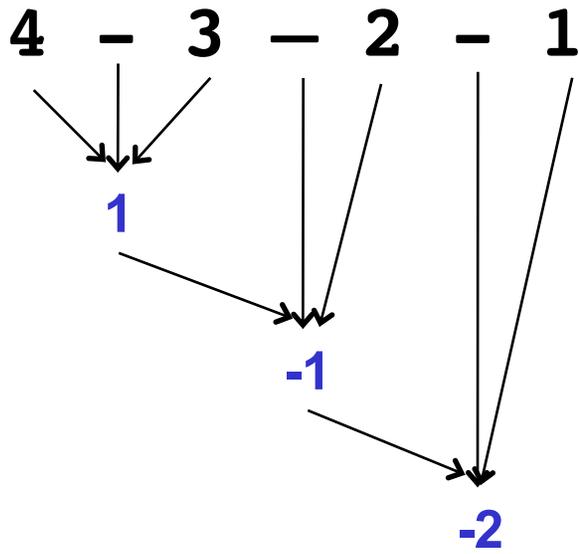


1.4 Building Bigger Expressions

- To understand how an expression is computed, we draw its *evaluation tree*
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- Expression is complete, and value is stored



1.4 Building Bigger Expressions



1.4 Building Bigger Expressions

- **These large and complicated expressions are truly pedagogical examples**
- **We write programs not only for the computer**
 - **But for other humans to understand**
- **The computer has no problem with large, complicated expressions**
 - **But we humans do!**
- **Better to write simpler, easier-to-read expressions**
 - **If it takes you time to understand what you wrote, then what you write is too complicated**
 - **A good test is to show a friend your code and get critical feedback about its quality and readability**

1.5 The `double` data type

- The `int` data type allows us to represent integer-valued items
 - How many students are in this class?
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 - How many words are in this sentence?
- **We sometimes need value beyond the decimal point**
 - The average age of students in this class
 - The probability of “heads” on a coin flip
- **We sometimes need really large or small values**
 - 6.0221413×10^{23} (Avagadro’s number)
 - 3×10^{-9} seconds (Time for light to travel one meter)

1.5 The `double` data type

- **The syntax is similar**
 - **The type is different (`double`)**
 - This is an unfortunate choice of name for a type
 - It refers to the amount of space used on a computer to represent the type.
 - We should think of it as a type that represents *rational* or *real* numbers

```
double secsPerMeter = .000000003;
```

1.5 The `double` data type

- **The syntax is similar**
 - **The type is different (`double`)**
 - **We can use scientific notation**
 - The E character represents “times 10 to the”
 - You can also specify the E as lower-case e

```
double secsPerMeter = 3E-9;
```

1.5 The double data type

- Most operations work as expected
 - + plus
 - - minus
 - * times
- As with `int`, division has some quirks for `double`
 - You can divide by 0
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1.5 The double data type

- **There are other surprises**
 - **The data type is inexact for some values**
 - **For nonrationals there is nothing we can do about this**
 - How would you represent “pi” exactly?
 - **For rationals, we can design a better data type**
 - But the fastest arithmetic on the computer is approximate in terms of values, as shown below
- **All of this is governed by an accepted standard**
 - **IEEE 754**

Expression	Value
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 - **Constants**
 - `Math.PI` – closer to the actual value of π than any other `double`
 - `Math.E` – closer to the actual value of e than any other `double`
- **Many, many more. See [this link](#)**

Roundtable

- **Randomness**
 - Run the random number generator and observe some of its outputs
 - Compute the average of 10 such numbers
- **Pseudo-random**
 - What does this mean?

1.6 Mixed-type Expressions

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 - Here we look at `int` and `double` types
- **If two types participate in an expression**
 - The result is usually of the more general type
- **The `double` type is more general than the `int` type**
 - We can represent any `int` as a `double`
 - For example, 3 becomes 3.0
 - But the converse is not true
 - No way to represent 0.5 as an `int`

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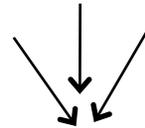
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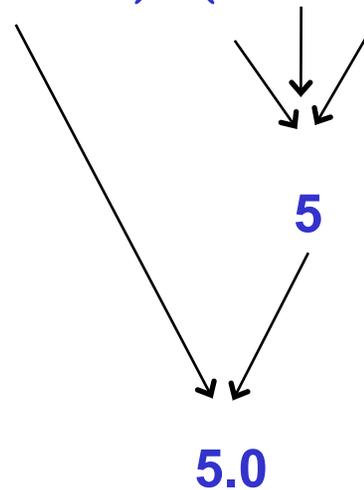


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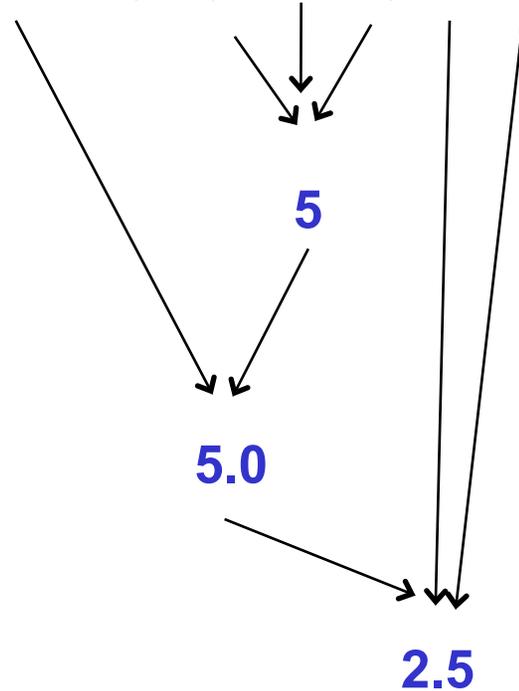
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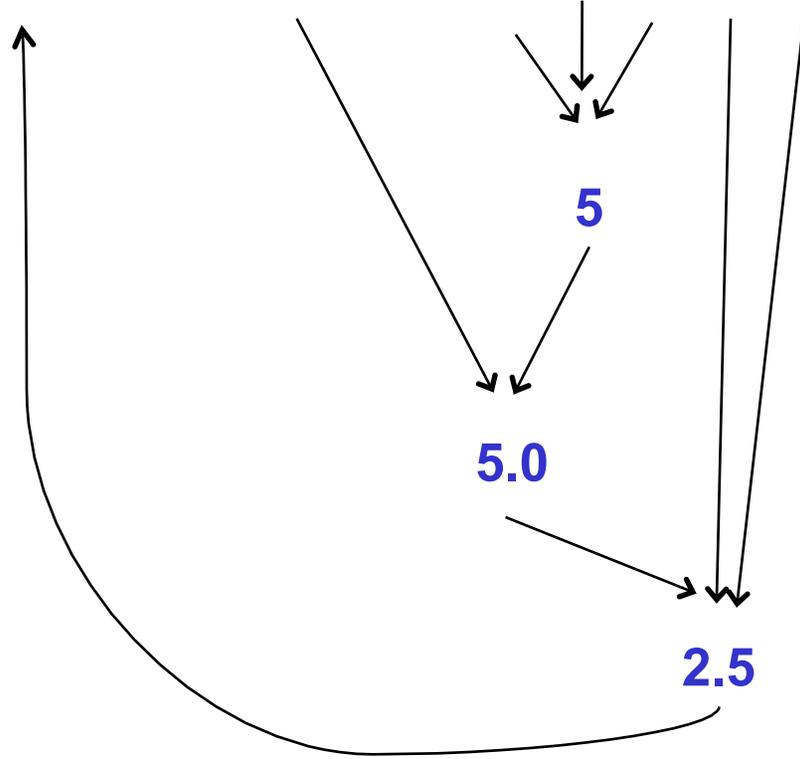
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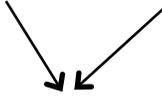
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`1.0`

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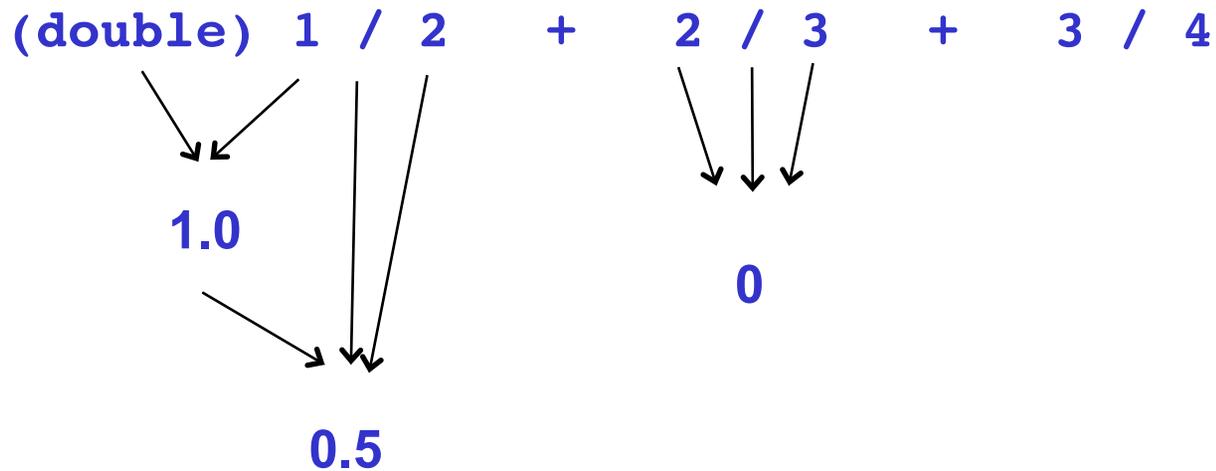
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The diagram illustrates the type promotion process. The expression is `(double) 1 / 2 + 2 / 3 + 3 / 4`. Arrows point from the `1` and `2` in the first term to the value `1.0`. Another arrow points from the `(double)` cast to the same `1.0`. A second set of arrows points from the `1`, `2`, `3`, and `4` in the remaining terms to the value `0.5`, indicating that these integer literals are promoted to `double` type.

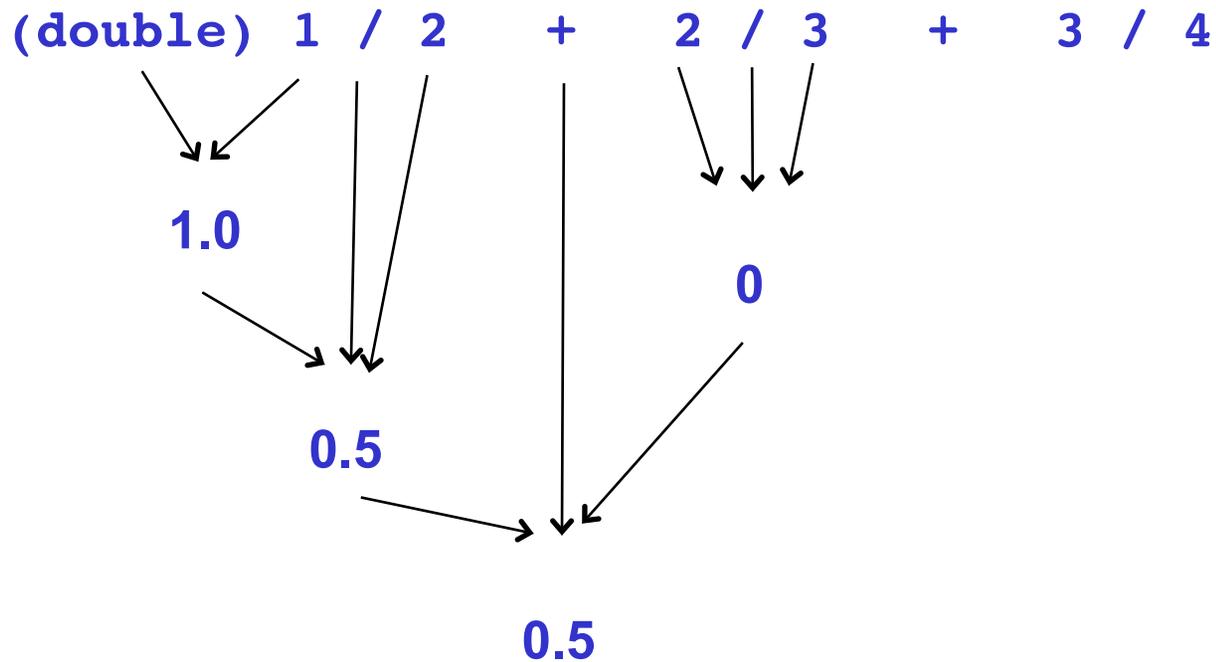
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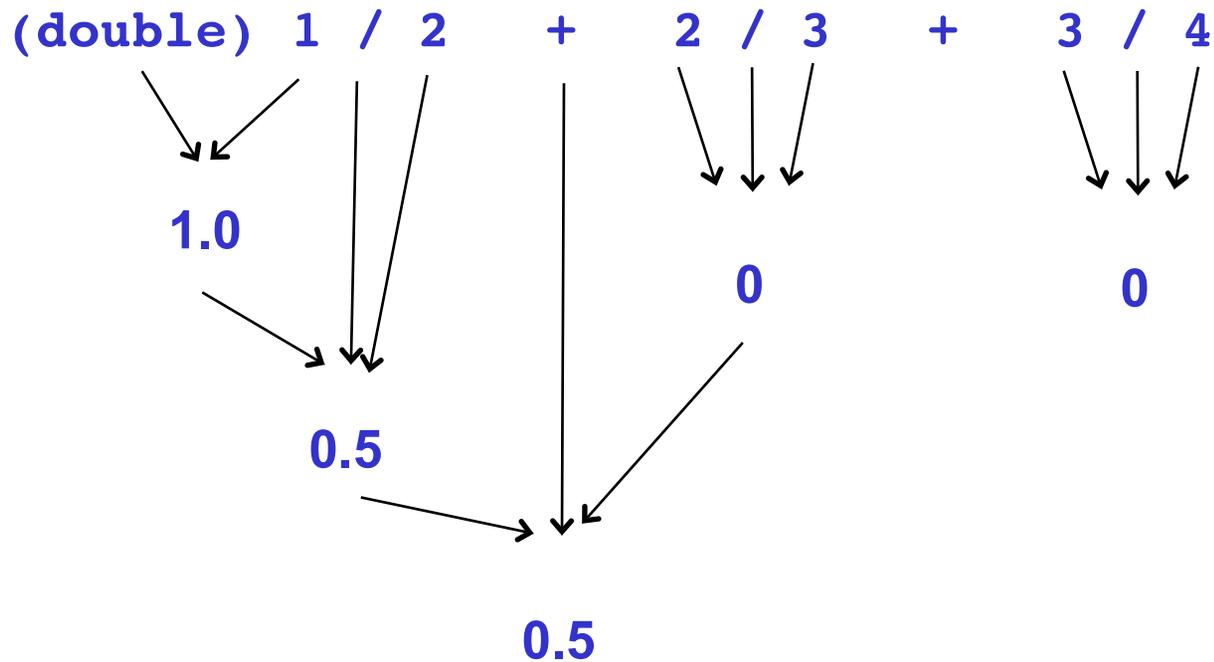
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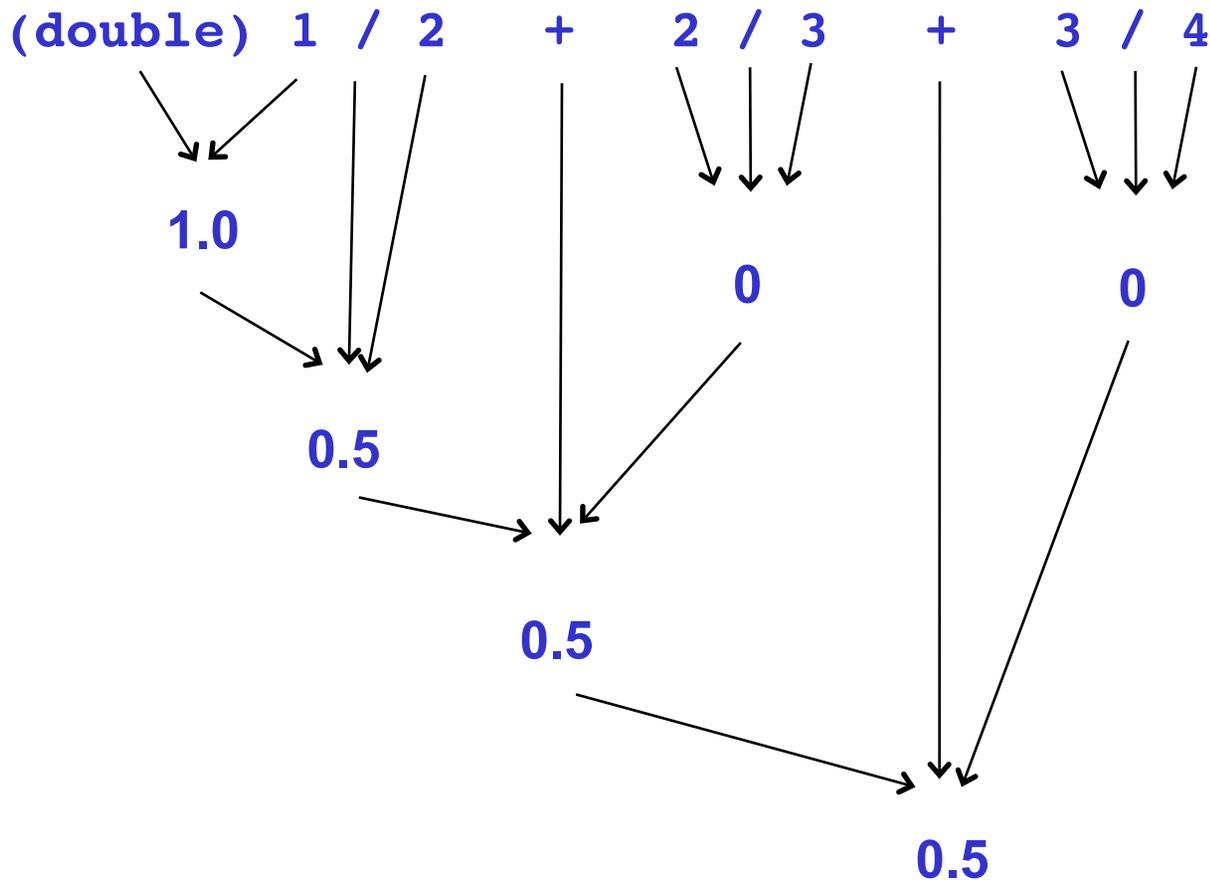
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Example	Result, if printed
"Hello" + "there"	Hellothere
"Hello " + "there"	Hello there
"" + "" + ""	

1.7 Strings

- **Declarations and assignments are the same as before.**

```
String s1 = "ei";
```

Variable Name	Value
s1	ei

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```

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String s1 = "ei";
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```
String s2 = s1 + s1;
```

```
String s3 = s2 + "o";
```

Variable Name	Value
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1.7 Strings

- **Conversion from other expression types to String produces the text form of their values.**
- **Given a String `s`, `s.length()` returns the length of the string in characters.**

Expression	Comments
<code>String size = 5;</code>	Not allowed

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<code>int length = msg.length();</code>	Returns the number of characters in the string. In this case, 6 is returned.

1.8 The boolean data type

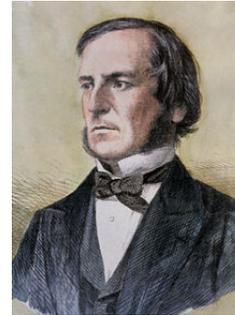
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1.8 The boolean data type

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 - **True vs. false**
 - **Heads vs. tails**
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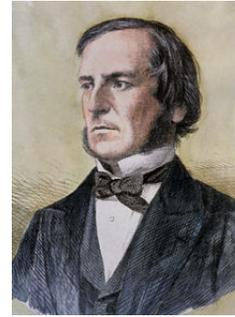
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 - True vs. false
 - Heads vs. tails
 - Open vs. closed
- **Named after George Bool**
 - 19th century logician and mathematician
 - But lower case *b* is important
- **Only two constants (lower case is important)**
 - true
 - false



1.8 The `boolean` data type

- **Mathematical operators work as expected, though some are spelled strangely**
 - `==` for equality
 - `!=` for inequality
 - `<=` for \leq , etc.

Expression	Value
<code>3 > 4</code>	<code>false</code>

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The usual rules of conversion apply here. The `int 7` is converted to the `double 7.0` and the comparison with `3.5` is then made.

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- **Logical operators are also available.**
 - **Complement**
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- **Logical operators are also available.**
 - **Complement**
 - `!p` is true if `p` is false
 - `!p` is false if `p` is true
 - **And**
 - `p && q` is true if *both* `p` and `q` have the value true
 - Works as expected for English meaning of *and*

1.8 The boolean data type

- **Logical operators are also available.**
 - **Complement**
 - `!p` is true if `p` is false
 - `!p` is false if `p` is true
 - **And**
 - `p && q` is true if *both* `p` and `q` have the value true
 - Works as expected for English meaning of *and*
 - **Or**
 - `p || q` is true if *either* `p` or `q` is true, or if *both* `p` and `q` are true
 - `p || q` is false only if `p` is false and `q` is false

1.8 The boolean data type

- **Logical operators are also available.**
 - **Complement**
 - `!p` is true if `p` is false
 - `!p` is false if `p` is true
 - **And**
 - `p && q` is true if *both* `p` and `q` have the value true
 - Works as expected for English meaning of *and*
 - **Or**
 - `p || q` is true if *either* `p` or `q` is true, or if *both* `p` and `q` are true
 - `p || q` is false only if `p` is false and `q` is false
 - This is different from the way we use *or* in English
 - I am going to the store or I am going to a movie
 - Means one or the other, but not both

1.8 The boolean data type

- **Examples**

p	q	Expression	Value
true		!p	false
false		!p	true

1.8 The boolean data type

- **Examples**

p	q	Expression	Value
true		!p	false
false		!p	true
true	false	p q	true

1.8 The boolean data type

- **Examples**

p	q	Expression	Value
true		!p	false
false		!p	true
true	false	p q	true
true	false	p && q	false

1.8 The boolean data type

- **Examples**

p	q	Expression	Value
true		!p	false
false		!p	true
true	false	p q	true
true	false	p && q	false
		p !p	true

1.8 The boolean data type

- **Examples**

p	q	Expression	Value
true		!p	false
false		!p	true
true	false	p q	true
true	false	p && q	false
		p !p	true
		p && !p	false

1.8 The boolean data type

- **Examples**

p	q	Expression	Value
true		!p	false
false		!p	true
true	false	p q	true
true	false	p && q	false
		p !p	true
		p && !p	false
true	true	p q	true

1.8 The boolean data type

- **Examples**

p	q	Expression	Value
true		!p	false
false		!p	true
true	false	p q	true
true	false	p && q	false
		p !p	true
		p && !p	false
true	true	p q	true
true	true	(p q) && !(p && q)	false

1.9 Conclusion

- **What is a *type*?**
 - **A classification of items in the world based on**
 - The kinds of things an item can do
 - The
 - **integers, real numbers, character strings, true/false values**
- **Types are also defined by the operations associated with them**
- **Data types in computer science**
 - **Represent values of interest**
 - **Allow operations that make sense**
- **Built in data types (in this module)**
 - **For representing integers, interest rates, names, addresses, facts**
- **Later, we design our own types**
 - **Bank account, hockey player, song**
- **The best choice of data type is not always obvious**
 - **You may start with one and change your mind later**
- **There are rarely right or wrong choices**
 - **But a choice will have its advantages and disadvantages**
 - **Picking a suitable data type is an engineering process and is based on currently understood constraints and best planning for the future. The future can at times seem uncertain.**