Wireless Physical Layer
Concepts: Part III

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Audio/Video recordings of this lecture are available at:
http://www.cse.wustl.edu/~jain/cse574-10/
Overview

1. Empirical Channel Models
2. Multi-Antenna Systems: Beam forming and MIMO
3. Space-Time Block Codes
4. Time Division Duplexing
5. OFDM, OFDMA, SOFDMA
Empirical Channel Models

Based on measured data in the field

1. Hata Model
2. COST 231 Extension to Hata Model
3. COST 231-Walfish-Ikegami Model
4. Erceg Model
5. Stanford University Interim (SUI) Models
6. ITU Path Loss Models
Hata Model

\[ P_{L,urban}(d)dB = 69.55 + 26.16\log_{10}(f_c) \\
-13.82\log_{10}(h_t) - a(h_r) + (44.9 - 6.55\log_{10}(h_t))\log_{10}(d) \]

- Based on 1968 measurement in Tokyo by Okumura
- Closed form expression by Hata in 1980
- \( f_c \) = carrier frequency,
  \( h_t \) = height of the transmitting (base station) antenna,
  \( h_r \) = height of the receiving (mobile) antenna
- \( a() \) = correction factor for the mobile antenna height based on the size of the coverage area
- Designed for 150-1500 MHz
COST 231 Extension to Hata Model

\[ P_{L,urban}(d)dB = 46.3 + 33.9\log_{10}(f_c) - 13.82\log_{10}(h_t) \]
\[ - a(h_r) + (44.9 - 6.55\log_{10}(h_t))\log_{10}(d) + C_M \]

- European Cooperative for Scientific and Technical (COST)
- Extended Hata model to 2 GHz:
- \( C_M \) = 0 dB for medium sized cities and suburbs
  = 3 dB for metropolitan areas
- Other Parameters:
  - Carrier Frequency: 1.5 GHz to 2 GHz
  - Base Antenna Height: 30 m to 300 m
  - Mobile Antenna Height: 1 m to 10 m
  - Distance: 1 km to 20 km
ITU Path Loss Models

- Indoor office, outdoor-to-indoor pedestrian, and vehicular. Low delay spread (A), medium delay spread (B)
- Pedestrian:

<table>
<thead>
<tr>
<th>Tap</th>
<th>Channel A</th>
<th>Channel B</th>
<th>Doppler spectrum</th>
</tr>
</thead>
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<tr>
<td></td>
<td>Relative delay (ns)</td>
<td>Average power (dB)</td>
<td>Relative delay (ns)</td>
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<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>2</td>
<td>110</td>
<td>–9.7</td>
<td>200</td>
</tr>
<tr>
<td>3</td>
<td>190</td>
<td>–19.2</td>
<td>800</td>
</tr>
<tr>
<td>4</td>
<td>410</td>
<td>–22.8</td>
<td>1 200</td>
</tr>
<tr>
<td>5</td>
<td>–</td>
<td>–</td>
<td>2 300</td>
</tr>
<tr>
<td>6</td>
<td>–</td>
<td>–</td>
<td>3 700</td>
</tr>
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</table>
## ITU Vehicular Channel Model

<table>
<thead>
<tr>
<th>Tap</th>
<th>Channel A</th>
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<th>Doppler spectrum</th>
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<td>Relative delay (ns)</td>
<td>Average power (dB)</td>
<td>Relative delay (ns)</td>
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<tr>
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<td>0</td>
<td>0.0</td>
<td>0</td>
</tr>
<tr>
<td>2</td>
<td>310</td>
<td>–1.0</td>
<td>300</td>
</tr>
<tr>
<td>3</td>
<td>710</td>
<td>–9.0</td>
<td>8.900</td>
</tr>
<tr>
<td>4</td>
<td>1 090</td>
<td>–10.0</td>
<td>12 900</td>
</tr>
<tr>
<td>5</td>
<td>1 730</td>
<td>–15.0</td>
<td>17 100</td>
</tr>
<tr>
<td>6</td>
<td>2 510</td>
<td>–20.0</td>
<td>20 000</td>
</tr>
</tbody>
</table>
Multi-Antenna Systems

- Receiver Diversity
- Transmitter Diversity
- Beam forming
- MIMO
Receiver Diversity

- User multiple receive antenna
- Selection combining: Select antenna with highest SNR
- Threshold combining: Select the first antenna with SNR above a threshold
- Maximal Ratio Combining: Phase is adjusted so that all signals have the same phase. Then weighted sum is used to maximize SNR
Transmitter Diversity

- Use multiple antennas to transmit the signal
  Ample space, power, and processing capacity at the transmitter (but not at the receiver).

- If the channel is known, phase each component and weight it before transmission so that they arrive in phase at the receiver and maximize SNR.

- If the channel is not known, use space time block codes.
Beam forming

- Phased Antenna Arrays: Receive the same signal using multiple antennas
- By phase-shifting various received signals and then summing ⇒ Focus on a narrow directional beam
- Digital Signal Processing (DSP) is used for signal processing ⇒ Self-aligning
MIMO

- Multiple Input Multiple Output
- RF chain for each antenna
  ⇒ Simultaneous reception or transmission of multiple streams

802.16e at 2.5 GHz, 10 MHz TDD, D:U=2:1

<table>
<thead>
<tr>
<th>T:R</th>
<th>1x1</th>
<th>1x2</th>
<th>2x2</th>
<th>2x4</th>
<th>4x2</th>
<th>4x4</th>
</tr>
</thead>
<tbody>
<tr>
<td>b/Hz</td>
<td>1.2</td>
<td>1.8</td>
<td>2.8</td>
<td>4.4</td>
<td>3.7</td>
<td>5.1</td>
</tr>
</tbody>
</table>
Space Time Block Codes (STBC)

- Invented 1998 by Vahid Tarokh.
- Transmit multiple redundant copies from multiple antennas
- Precisely coordinate distribution of symbols in space and time.
- Receiver combines multiple copies of the received signals optimally to overcome multipath.
- Example: Two antennas:

Antenna 1

\[
\begin{pmatrix}
S_1 \\
-S_2^* 
\end{pmatrix}
\]

Antenna 2

\[
\begin{pmatrix}
S_2 \\
S_1^* 
\end{pmatrix}
\]

S1* is complex conjugate of S1 \(\Rightarrow\) columns are orthogonal
Time Division Duplexing (TDD)

- Duplex = Bi-Directional Communication
- Frequency division duplexing (FDD) (Full-Duplex)
  - Frequency 1
  - Frequency 2
- Time division duplex (TDD): Half-duplex
  - Base
  - Subscriber
- Most WiMAX deployments will use TDD.
  - Allows more flexible sharing of DL/UL data rate
  - Does not require paired spectrum
  - Easy channel estimation ⇒ Simpler transceiver design
  - Con: All neighboring BS should time synchronize
Inter-Symbol Interference

- Symbols become wider
  ⇒ Limits the number of bits/s
OFDM

- Orthogonal Frequency Division Multiplexing
- Ten 100 kHz channels are better than one 1 MHz Channel
  ⇒ Multi-carrier modulation
- Frequency band is divided into 256 or more sub-bands. Orthogonal ⇒ Peak of one at null of others
- Each carrier is modulated with a BPSK, QPSK, 16-QAM, 64-QAM etc depending on the noise (Frequency selective fading)
- Used in 802.11a/g, 802.16, Digital Video Broadcast handheld (DVB-H)
- Easy to implement using FFT/IFFT
Advantages of OFDM

- Easy to implement using FFT/IFFT
- Computational complexity = $O(B \log BT)$ compared to previous $O(B^2T)$ for Equalization. Here $B$ is the bandwidth and $T$ is the delay spread.
- Graceful degradation if excess delay
- Robustness against frequency selective burst errors
- Allows adaptive modulation and coding of subcarriers
- Robust against narrowband interference (affecting only some subcarriers)
- Allows pilot subcarriers for channel estimation
OFDM: Design considerations

- Large number of carriers ⇒ Smaller data rate per carrier ⇒ Larger symbol duration ⇒ Less inter-symbol interference
- Reduced subcarrier spacing ⇒ Increased inter-carrier interference due to Doppler spread in mobile applications
- Easily implemented as Inverse Discrete Fourier Transform (IDFT) of data symbol block
- Fast Fourier Transform (FFT) is a computationally efficient way of computing DFT

10 Mbps

0.1 μs

1 Mbps

1 μs
OFDMA

- Orthogonal Frequency Division Multiple Access
- Each user has a subset of subcarriers for a few slots
- OFDM systems use TDMA
- OFDMA allows Time+Freq DMA $\Rightarrow$ 2D Scheduling
Scalable OFDMA (SOFDMA)

- OFDM symbol duration = f(subcarrier spacing)
- Subcarrier spacing = Frequency bandwidth/Number of subcarriers
- Frequency bandwidth = 1.25 MHz, 3.5 MHz, 5 MHz, 10 MHz, 20 MHz, etc.
- Symbol duration affects higher layer operation
  ⇒ Keep symbol duration constant at 102.9 us
  ⇒ Keep subcarrier spacing 10.94 kHz
  ⇒ Number of subcarriers ∝ Frequency bandwidth

This is known as scalable OFDMA
Summary: Wireless PHY Part III

1. Empirical Channel models give path loss based on measured data
2. Multiple Antennas: Receive diversity, transmit diversity, Smart Antenna, MIMO
3. MIMO use multiple antennas for high throughput
4. Space-time block codes use multiple antennas to transmit related signals
5. OFDM splits a band into many orthogonal subcarriers. OFDMA = FDMA + TDMA
Homework 5

In a scalable OFDMA system, the number of carriers for 10 MHz channel is 1024. How many carriers will be used if the channel was 1.25 MHz, 5 MHz, or 8.75 MHz.
Reading List

- R. Jain, “Channel Models: A Tutorial,”
- Hata Model,
- Cost 231 Model,
- Space-Time Block Codes,