Block Encryption and DES

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Audio/Video recordings of this lecture are available at:
http://www.cse.wustl.edu/~jain/cse571-17/
Overview

1. Substitution and Transposition Techniques
2. Block Cipher Principles
3. Data Encryption Standard (DES)
4. Differential and Linear Cryptanalysis
5. Block Cipher Design Principles

Symmetric Cipher Model

\[ Y = E(K, X) \]
\[ X = D(K, Y) \]

K=Secret Key

Same key is used for encryption and decryption.

⇒ Single-key or private key encryption.

Example: Divide by 9. \( 480 = 53 \times 9 + 3 \Rightarrow 533 \)
Some Basic Terminology

- **Plaintext**: original message
- **Ciphertext**: coded message
- **Cipher**: algorithm for transforming plaintext to ciphertext
- **Key**: info used in cipher known only to sender/receiver
- **Encipher (encrypt)**: converting plaintext to ciphertext
- **Decipher (decrypt)**: recovering ciphertext from plaintext
- **Cryptography**: study of encryption principles/methods
- **Cryptanalysis (code breaking)**: study of principles/methods of deciphering ciphertext without knowing key
- **Cryptology**: field of both cryptography and cryptanalysis
Substitution

- **Caesar Cipher**: Replaces each letter by 3rd letter on
  - Example:
    ```
    meet me after the toga party
    PHHW PH DIWHU WKH WRJD SDUWB
    ```
  - Can define transformation as:
    ```
    a b c d e f g h i j k l m n o p q r s t u v w x y z
    D E F G H I J K L M N O P Q R S T U V W X Y Z
    ```
  - Mathematically give each letter a number
    ```
    a b c d e f g h i j k l m n o p q r s t u v w x y z
    0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25
    ```
  - Then have Caesar cipher as:
    ```
    c = E(k, p) = (p + k) \mod (26)
    p = D(k, c) = (c – k) \mod (26)
    ```
  - Weakness: Only 26 possible keys
Substitution: Other forms

- Random substitution:
  Plain:  abcdefghijklmnopqrstuvwxyz
  Cipher: DKVQFIBJWPESCXHTMYAUOLRGZN

  The key is 26 character long
  => 26! (= 4 x 10^{26}) Keys in place of 26 keys

- Letter frequencies to find common letters: E,T,R,N,I,O,A,S
Substitution: Other forms (Cont)

- Use two-letter combinations: Playfair Cipher
- Use multiple letter combinations: Hill Cipher
- **Poly-alphabetic Substitution Ciphers**
  - Use multiple ciphers. Use a key to select which alphabet (code) is used for each letter of the message
  - **Vigenère Cipher**: Example using keyword *deceptive*
    - key:  deceptive
deceptivedeceptivedeceptivedeceptive
    - plaintext: wearediscoverededsaveyourself
ciphertext: ZICVTWQNGRZGVTWAVZHCQYGLMGJ
Transposition (Permutation) Ciphers

- Rearrange the letter order without altering the actual letters

- **Rail Fence Cipher**: Write message out diagonally as:
  
  mem a t r h t g p r y
e t e f e t e o a a t

  Giving ciphertext: MEMATRHTGPRYETEFETEOAAT

- **Row Transposition Ciphers**: Write letters in rows, reorder the columns according to the key before reading off.
  
  Key: 4312567
  Column Out 4 3 1 2 5 6 7
  Plaintext: a t t a c k p
  o s t p o n e
d u n t i l t
  w o a m x y z

  Ciphertext: TTNAAPTMTSUOAODWCOIXKNLYPETZ
Product Ciphers

- Use several ciphers in succession to make harder, but:
  - Two substitutions make a more complex substitution
  - Two transpositions make more complex transposition
  - But a substitution followed by a transposition makes a much harder cipher

- This is a bridge from classical to modern ciphers
This problem explores the use of a one-time pad version of the Vigenere cipher. In this scheme, the key is a stream of random numbers between 0 and 26. For example, if the key is 3 19 5…, then the first letter of the plaintext is encrypted with a shift of 3 letters, the second with a shift of 19 letters, the third with a shift of 5 letters, and so on.

A. Encrypt the plain text sendmoremoney with the key stream 9 0 1 7 23 15 21 14 11 11 2 8 9

B. Using the ciphertext produced in part (a), find a key so that the cipher text decrypts to the plain text cashnotneeded.
Block vs. Stream Ciphers

- **Stream**: Bits and bytes are processed as they arrive
  Example: RC4

- **Block**: Messages are broken into blocks of 64-bit, 512-bit, …
  Example: DES, AES
Shannon’s S-P Networks

- Claude Shannon introduced the idea of substitution-permutation (S-P) networks in his 1949 paper.

- Two primitive cryptographic operations:
  - **Substitution (S-box)** = Replace n-bits by another n-bits.
    - **Diffusion**: Dissipate statistical structure of plaintext over bulk of ciphertext. One bit change in plaintext changes many bits in ciphertext. Can not do frequency analysis.
  - **Permutation (P-box)** = Bits are rearranged.
    - No bits are added/removed.
    - **Confusion**: Make relationship between ciphertext and key as complex as possible.

- Combination S-P = Product cipher
Feistel Cipher Structure

- A practical implementation of Shannon's S-P Networks
- Partitions input block in 2 halves
  - Perform a substitution on left data half based on a function of right half & subkey (Round Function or Mangler function)
  - Then permutation by swapping halves
  - Repeat this “round” of S-P many times
- Invertible
Feistel Cipher Design Elements

Most modern block ciphers are a variation of Feistel Cipher with different:

1. Block size
2. Key size
3. Number of rounds
4. Subkey generation algorithm
5. Round function
6. Fast software en/decryption
7. Ease of analysis
Data Encryption Standard (DES)

- Published by NIST in 1977
- A variation of IBM’s Lucifer algorithm developed by Horst Feistel
- For commercial and unclassified government applications
- 8 octet (64 bit) key.
  - Each octet with 1 odd parity bit $\Rightarrow$ 56-bit key
- Efficient hardware implementation
- Used in most financial transactions
- Computing power goes up 1 bit every 2 years
- 56-bit was secure in 1977 but is not secure today
- Now we use DES three times $\Rightarrow$ Triple DES = 3DES
DES Encryption Overview

- 16 rounds using 64-bit block and 48-bit subkey

1. Initial/Final Permutation
2. Round Function
3. Sub-key Generation
1. Initial and Final Permutation

<table>
<thead>
<tr>
<th>Initial Permutation (IP)</th>
<th>Final Permutation (IP⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>58 50 42 34 26 18 10 2</td>
<td>40 8 48 16 56 24 64 32</td>
</tr>
<tr>
<td>60 52 44 36 28 20 12 4</td>
<td>39 7 47 15 55 23 63 31</td>
</tr>
<tr>
<td>62 54 46 38 30 22 14 6</td>
<td>38 6 46 14 54 22 62 30</td>
</tr>
<tr>
<td>64 56 48 40 32 24 16 8</td>
<td>37 5 45 13 53 21 61 29</td>
</tr>
<tr>
<td>57 49 41 33 25 17 9 1</td>
<td>36 4 44 12 52 20 60 28</td>
</tr>
<tr>
<td>59 51 43 35 27 19 11 3</td>
<td>35 3 43 11 51 19 59 27</td>
</tr>
<tr>
<td>61 53 45 37 29 21 13 5</td>
<td>34 2 42 10 50 18 58 26</td>
</tr>
<tr>
<td>63 55 47 39 31 23 15 7</td>
<td>33 1 41 9 49 17 57 25</td>
</tr>
</tbody>
</table>

- Input bit 58 goes to output bit 1
  Input bit 50 goes to output bit 2, ...
- Even bits to Left half, odd bits to Right half
- Quite regular in structure (easy in h/w)
2. DES Round Structure

Read 6 bits. Go back 2 bits. Repeat.

Substitution Boxes

Permutation
Substitution Boxes

- Map 6 to 4 bits
- Outer bits 1 & 6 (row bits) select one row of 4
- Inner bits 2-5 (column bits) are substituted
- Example:

<table>
<thead>
<tr>
<th>Input bits 1 and 6</th>
<th>Input bits 2 thru 5</th>
</tr>
</thead>
<tbody>
<tr>
<td>↓</td>
<td></td>
</tr>
<tr>
<td>00</td>
<td>1110 0100 1101 0001</td>
</tr>
<tr>
<td>01</td>
<td>0000 1111 0110 1101</td>
</tr>
<tr>
<td>10</td>
<td>0100 0001 1110 1001</td>
</tr>
<tr>
<td>11</td>
<td>1111 1100 1000 0010</td>
</tr>
<tr>
<td>00</td>
<td>0010 0101 0110 0111</td>
</tr>
<tr>
<td>01</td>
<td>1000 1011 1100 1011</td>
</tr>
<tr>
<td>10</td>
<td>1010 0101 1011 1111</td>
</tr>
<tr>
<td>11</td>
<td>1110 1010 0000 0110</td>
</tr>
</tbody>
</table>
3. DES Sub-Key Generation

- Permutation PC1 divides 56-bits into two 28-bit halves.
- Rotate each half separately either 1 or 2 places depending on the key rotation schedule K.
- Select 24-bits from each half & permute them by PC2.
DES Decryption

- Decrypt with Feistel design: Do encryption steps again using sub-keys in reverse order (SK16 … SK1)
  - IP undoes final FP step of encryption
  - 1st round with SK16 undoes 16th encrypt round
  - ….
  - 16th round with SK1 undoes 1st encrypt round
  - Then final FP undoes initial encryption IP thus recovering original data value
Avalanche Effect

- Key desirable property of encryption algorithm
- A change of one input or key bit results in changing approx half output bits = Diffusion
- Making attempts to “home-in” by guessing keys impossible
- DES exhibits strong avalanche
### Avalanche in DES

<table>
<thead>
<tr>
<th>Round</th>
<th>02468aceeca86420 12468aceeca86420</th>
<th>( \delta )</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3cf03c0fbad22845 3cf03c0fbad32845</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>bad2284599e9b723 bad3284539a9b7a3</td>
<td>5</td>
</tr>
<tr>
<td>3</td>
<td>99e9b7230bae3b9e 39a9b7a3171cb8b3</td>
<td>18</td>
</tr>
<tr>
<td>4</td>
<td>0bae3b9e42415649 171cb8b3ccaca55e</td>
<td>34</td>
</tr>
<tr>
<td>5</td>
<td>4241564918b3fa41 ccaca55ed16c3653</td>
<td>37</td>
</tr>
<tr>
<td>6</td>
<td>18b3fa419616fe23 d16c3653cf402c68</td>
<td>33</td>
</tr>
<tr>
<td>7</td>
<td>9616fe2367117cf2 cf402c682b2ceefbc</td>
<td>32</td>
</tr>
<tr>
<td>8</td>
<td>67117cf2c11bfc09 2b2ceefbc99f91153</td>
<td>33</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Round</th>
<th>c11bfc09887fbc6c 99f911532eed7d94</th>
</tr>
</thead>
<tbody>
<tr>
<td>9</td>
<td>887fbc6c600f7e8b 2eed7d94d0f23094</td>
</tr>
<tr>
<td>10</td>
<td>600f7e8bf596506e d0f23094455da9c4</td>
</tr>
<tr>
<td>11</td>
<td>f596506e738538b8 455da9c47f6e3cf3</td>
</tr>
<tr>
<td>12</td>
<td>738538b8c6a62c4e 7f6e3cf34bc1a8d9</td>
</tr>
<tr>
<td>13</td>
<td>c6a62c4e56b0bd75 4bc1a8d91e07d409</td>
</tr>
<tr>
<td>14</td>
<td>56b0bd7575e8fd8f 1e07d4091ce2e6dc</td>
</tr>
<tr>
<td>15</td>
<td>75e8fd8f25896490 1ce2e6dc365e5f59</td>
</tr>
<tr>
<td>16</td>
<td>da02ce3a89ecac3b 057cde97d7683f2a</td>
</tr>
</tbody>
</table>

\[3+4+3+3+1+0+2+3+2+3+1+2+2+2+1+1 = 33 \text{ bits}\]
Strength of DES

- Bit-wise complement of plaintext with complement of key results in complement of ciphertext
- Brute force search requires $2^{55}$ keys
- Recent advances have shown, it is possible
  - in 1997 on Internet in a few months
  - in 1998 on dedicated h/w (EFF) in a few days
  - in 1999 above combined in 22hrs!
- Statistical Attacks:
  - Timing attacks: calculation time depends upon the key. Particularly problematic on smartcards
  - Differential cryptanalysis
  - Linear cryptanalysis
Differential Cryptanalysis

- Chosen Plaintext attack: Get ciphertext for a given plaintext
- Get the \((\Delta X, \Delta Y)\) pairs, where \(\Delta X\) is the difference in plaintext and \(\Delta Y\) is the difference in ciphertext
- Some \((\Delta X, \Delta Y)\) pairs are more likely than others, if those pairs are found, some key values are more likely so you can reduce the amount of brute force search
- Straightforward brute force attack on DES requires \(2^{55}\) plaintexts
- Using differential cryptanalysis, DES can be broken with \(2^{47}\) plaintexts.
  But finding appropriate plaintexts takes some trials and so the total amount of effort is \(2^{55.1}\) which is more than straightforward brute force attack
  \(\Rightarrow\) DES is resistant to differential cryptanalysis

Linear Cryptanalysis

- Bits in plaintext, ciphertext, and keys may have a linear relationship. For example:
  \[ P_1 \oplus P_2 \oplus C_3 = K_2 \oplus K_5 \]

- In a good cipher, the relationship should hold with probability \( \frac{1}{2} \). If any relationship has probability 1, the cipher is easy to break. If any relationship has probability 0, the cipher is easy to break.

- **Bias** = |Probability of linear relationship – 0.5|

- Find the linear approximation with the highest bias
  \[ \Rightarrow \text{Helps reduce the brute force search effort.} \]

- This method can be used to find the DES key given \( 2^{43} \) plaintexts.

Ref: [http://en.wikipedia.org/wiki/Linear_cryptanalysis](http://en.wikipedia.org/wiki/Linear_cryptanalysis)
Block Cipher Design Principles

- **Nonlinear S-Boxes**: Resistant to linear cryptanalysis. Linear approximations between input and output bits of the S-boxes should have minimal bias \( P \approx \frac{1}{2} \)

- S-Boxes resistant to differential cryptanalysis. All (input bit difference, output bit difference) pairs should be equally likely.

- Any output bit should change with probability \( \frac{1}{2} \) when any input bit is changed (strict avalanche criterion)

- Output bits \( j \) and \( k \) should change independently when any input bit \( i \) is inverted for all \( i, j, k \) (bit independence criterion)

- **Permutation**: Adjacent bits should affect different S-Boxes in the next round \( \Rightarrow \) Increase diffusion

- More rounds are better (but also more computation)
Summary

1. The key methods for cryptography are: Substitution and transposition

2. Letter frequency can be used to break substitution

3. Goal of ciphers is to increase confusion and diffusion. Confusion = Complex relationship Diffusion = Each input bit affects many output bits

4. Feistel cipher design divides blocks in left and right halves, mangles the right half with a sub-key and swaps the two halves.

5. DES consists of 16 rounds using a 56-bit key from which 48-bit subkeys are generated. Each round uses eight 6x4 S-Boxes followed by permutation.

6. Differential cryptanalysis analyzes frequency of $(\Delta P, \Delta C)$ pairs. Linear cryptanalysis analyzes frequency of linear relationships among plaintext, ciphertext, and key.
Homework 2B

Suppose we use one round version of DES.
1. Derive $K_1$, the first-round subkey
2. Derive $L_0$, $R_0$
3. Expand $R_0$ to get $E[R_0]$, where $E[.]$ is the expansion function of Table S.1
4. Calculate $A = E[R_0] \oplus K_1$
5. Group the 48-bit result above into sets of 6 bits and evaluate the corresponding S-Box substitution
6. Concatenate the results above to get a 32-bit result, $B$.
7. Apply the permutation to get $P(B)$
8. Calculate $R_1 = P(B) \oplus L_0$
9. Write down the ciphertext.

Final Answer: $F0AAF0AA \ 5E1CEC63$
Acronyms

- 3DES  | Triple Data Encryption Standard
- AES   | Advanced Encryption Standard
- ASCII | American Standard Code for Information Interchange
- CIA   | Confidentiality, Integrity, and Availability
- DES   | Data Encryption Standard
- EFF   | Electronic Frontier Foundation
- FP    | Final Permutation
- IP    | Initial Permutation
- LH    | Left-Half
- NIST  | National Institute of Standards and Technology
- NSA   | National Security Agency
- PCn   | Permuted Choice n
- RC4   | Ron's Code 4
- RH    | Right-Half
- SKn   | Sub-Key n
Related Modules

CSE571S: Network Security (Spring 2017),
http://www.cse.wustl.edu/~jain/cse571-17/index.html

CSE473S: Introduction to Computer Networks (Fall 2016),
http://www.cse.wustl.edu/~jain/cse473-16/index.html

Wireless and Mobile Networking (Spring 2016),
http://www.cse.wustl.edu/~jain/cse574-16/index.html

CSE571S: Network Security (Fall 2014),
http://www.cse.wustl.edu/~jain/cse571-14/index.html

Audio/Video Recordings and Podcasts of Professor Raj Jain's Lectures,
https://www.youtube.com/channel/UCN4-5wzNP9-ruOzQMs-8NUw