

---

# Aggregation of MIMO Latency

Arjan Durreesi, Raj Jain, Gojko Babic

The Ohio State University

Contact: Jain@cis.ohio-state.edu

These slides are available at

[http://www.cis.ohio-state.edu/~jain/atmf/af\\_mimo.htm](http://www.cis.ohio-state.edu/~jain/atmf/af_mimo.htm)



Desired Properties of Metrics

FILO, LILO Latency Issues

MIMO Latency: Definition and Examples

MIMO vs LILO

Measurement Results

MIMO Latency of a Path

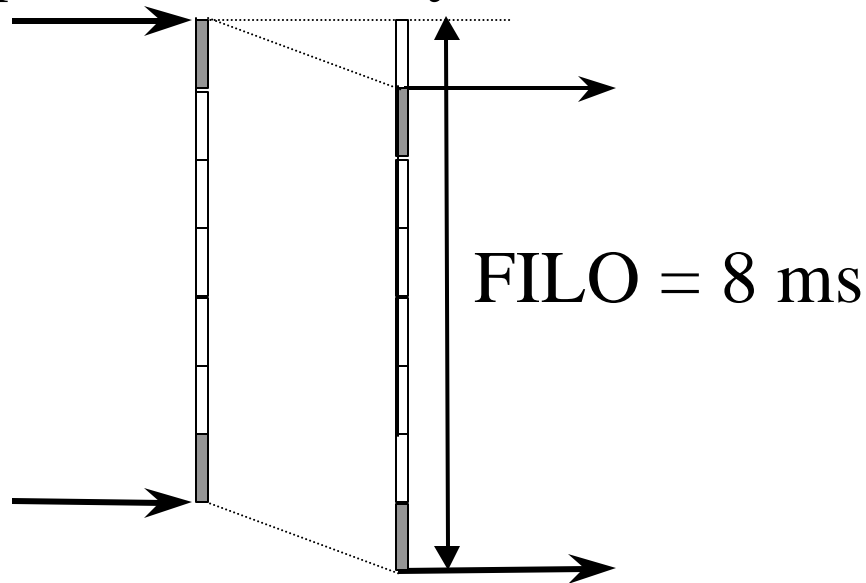
---

# Desired Properties of Metrics

Measured performance = Function{System, Workload}

Metrics that depend highly on workload and less on the system are undesirable

Example 2: Gap = 5 ms. Delay = 1 ms  $\Rightarrow$  FILO = 8 ms

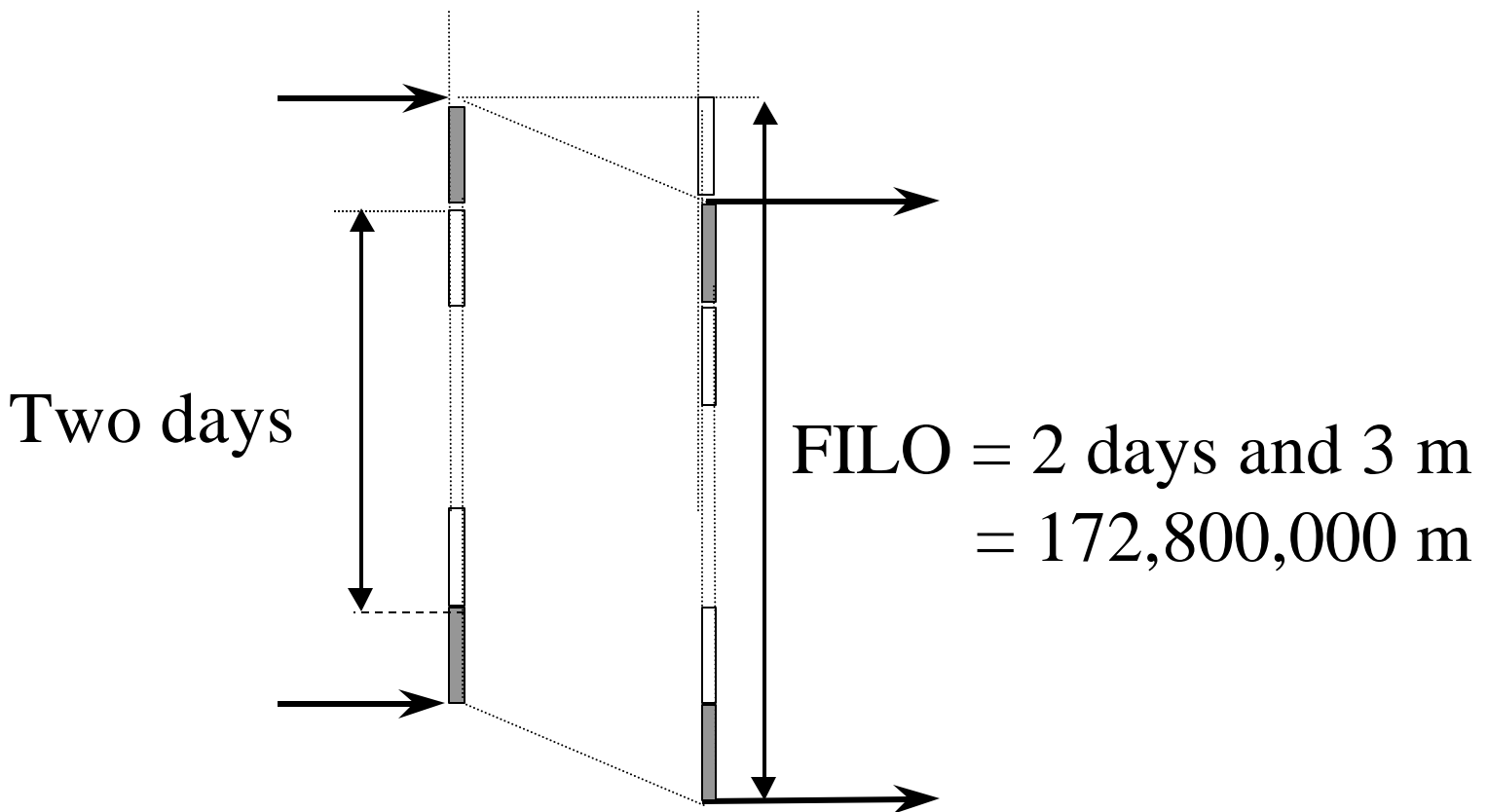


---

# ILO Latency: Another Example

Example 2: Gap = 2 days. Delay = 1 ms.

⇒ FILO = 2 days + 3 ms

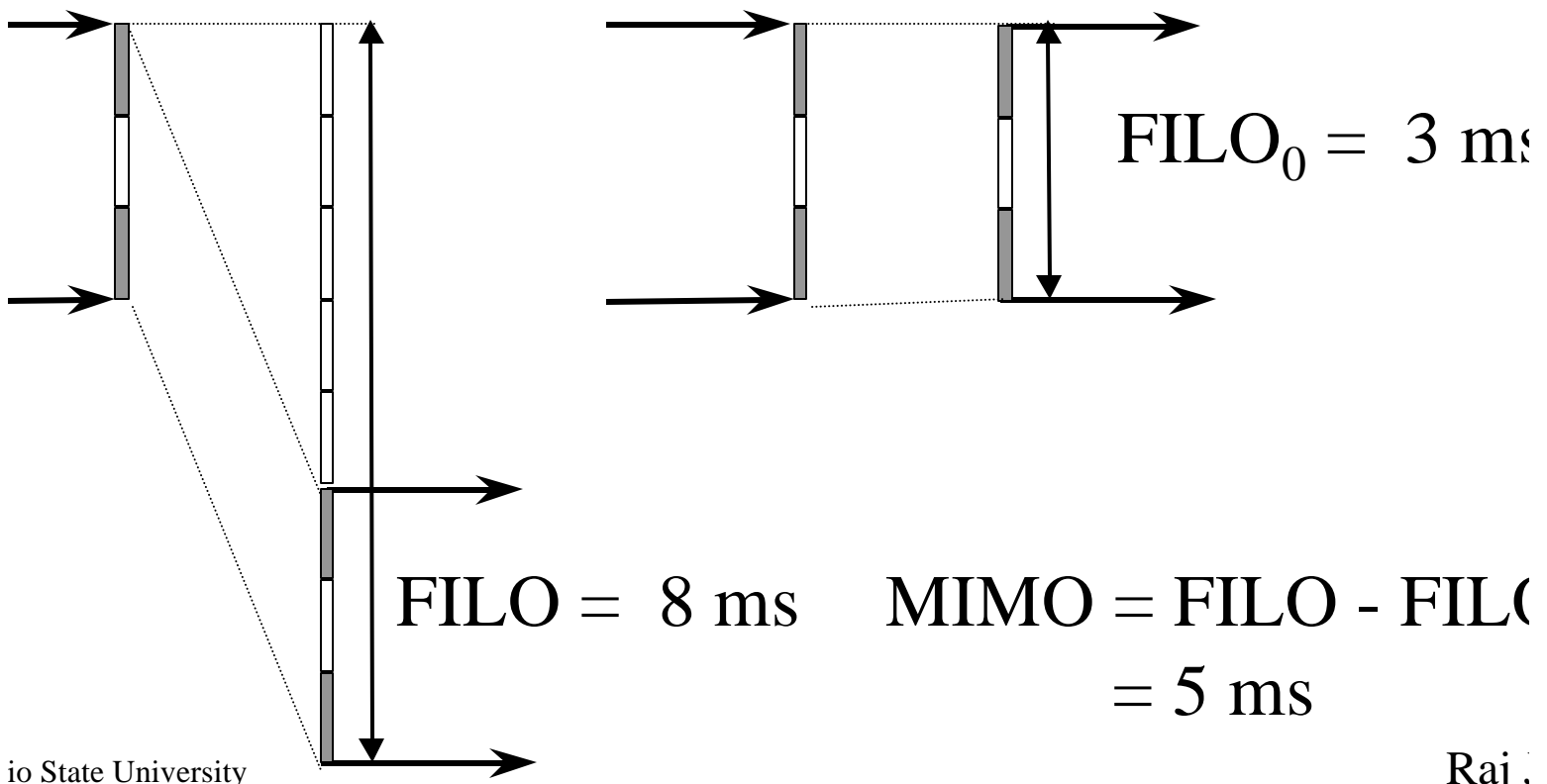


# MIMO Latency: Definition

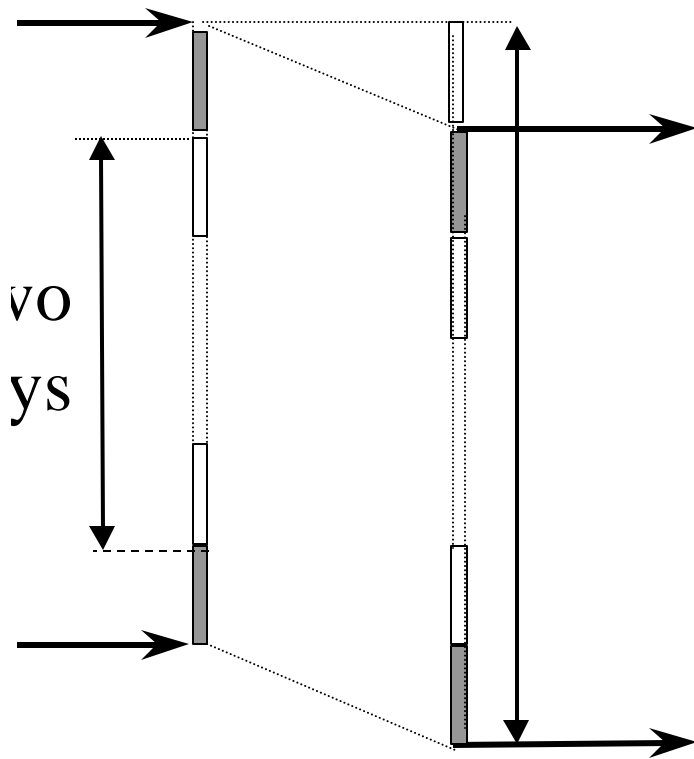
$$\text{MIMO Latency} = \text{FILO} - \text{FILO}_0$$

$\text{FILO}_0$  = FILO latency through an ideal network

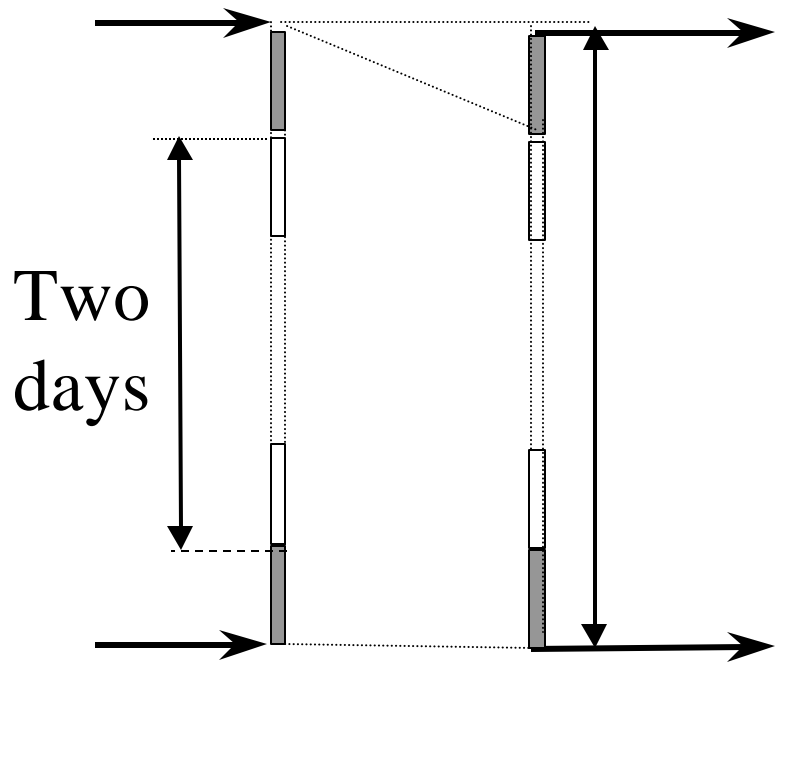
Ideal Network = Zero length wire (in many cases)



# MIMO Latency: Example 2



$$\text{FILO} = 2 \text{ days} + 3 \text{ ms}$$



$$\text{FILO}_0 = 2 \text{ days} + 2 \text{ ms}$$

$$\text{MIMO Latency} = \text{FILO} - \text{FILO}_0 = 1 \text{ ms}$$

---

# Another Equivalent Definition

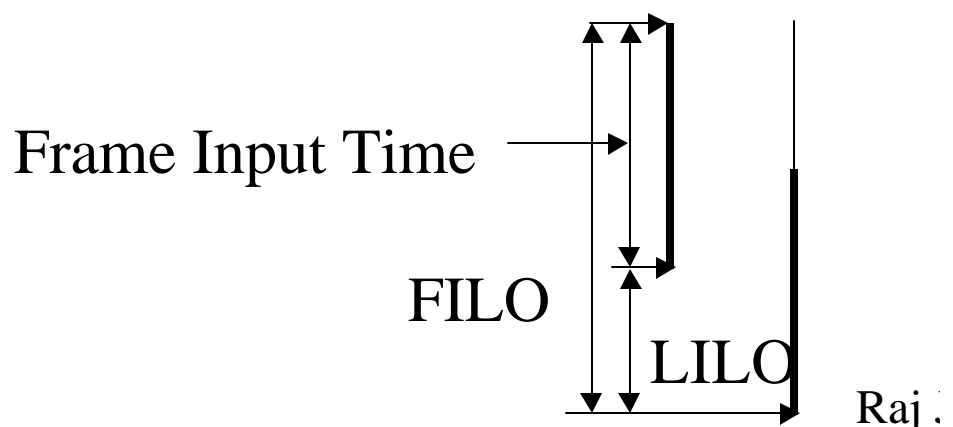
First Definition:  $MIMO = FILO - FILO_0$ .

ex “0” indicates zero-delay switch

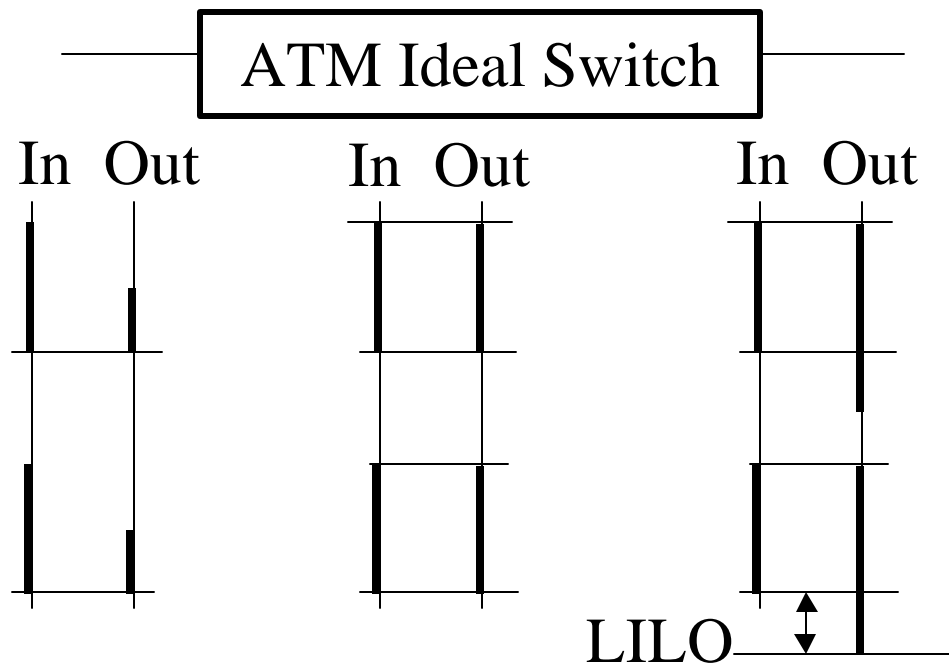
Definition of FILO:

- $FILO = \text{Frame Input Time} + LILO$
- $FILO_0 = \text{Frame Input Time} + LILO_0$

Second Definition:  $MIMO = LILO_{IN} - LILO_{OUT}$



# Delay Through an Ideal Switch



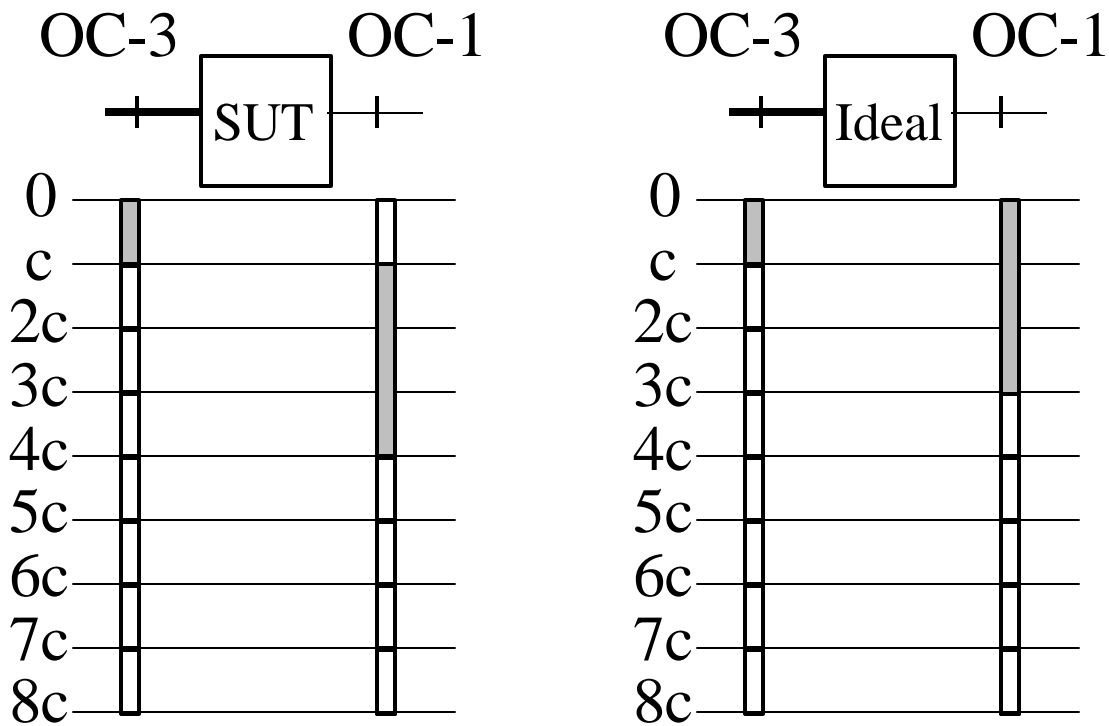
$$\text{LILO}_0 = 0$$

if input speed  $\leq$  output speed

$$\text{LILO}_0 > 0$$

iff input speed  $>$  output speed

# MIMO vs LILO: 1-Cell Frame

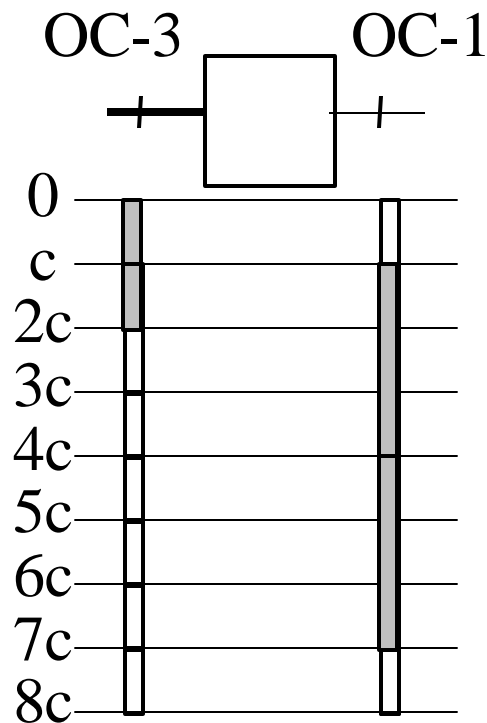


Consider a switch with one cell delay

- LILO = 3c, LILO<sub>0</sub> = 2c, MIMO = 1c

---

# MIMO vs LILO: 2-Cell Frame

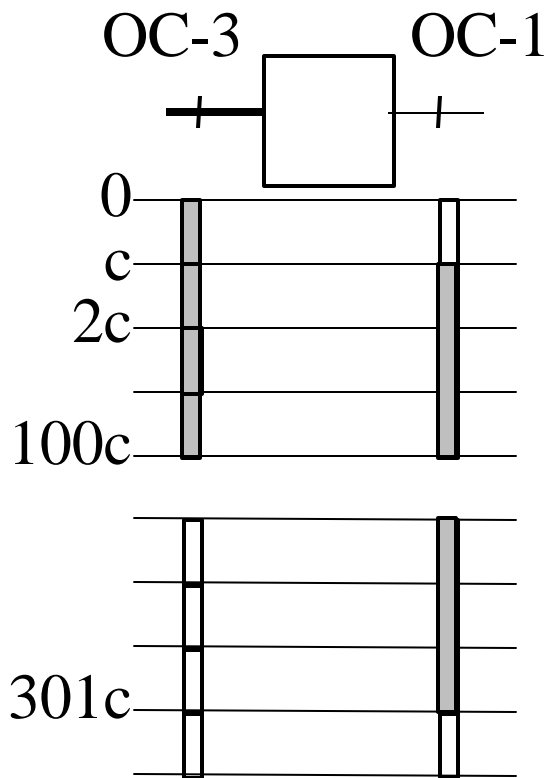


Consider a switch with one cell delay

- LILO =  $5c$ , LILO<sub>0</sub> =  $4c$ , MIMO =  $1c$

---

# MIMO vs LILO: 100-Cell Fram



Consider a switch with one cell delay

- LILO = 301c, LILO<sub>0</sub> = 300c, MIMO = 1c

---

# MIMO vs LILO

Frame Size	LILO	LILO0	MIMO
1c	4c	3c	1c
10c	31c	30c	1c
100c	301c	300c	1c
1,000c	3,001c	3,000c	1c
10,000c	30,001c	30,000c	1c
10,0000c	30,0001c	300,000c	1c

---

# MIMO vs LILO

$$\text{MIMO} = \text{LILO} - \text{LILO}_0$$

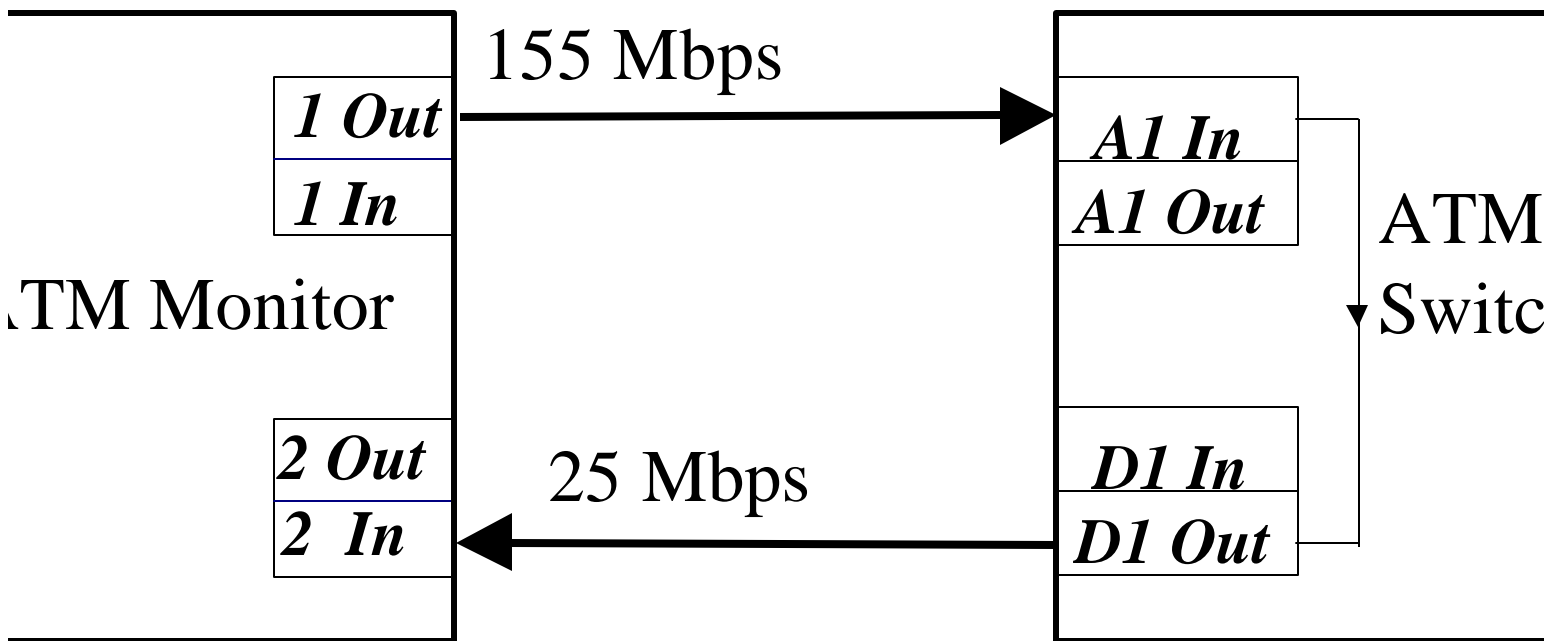
- LILO measures the total delay.
- $\text{LILO}_0$  measures the workload dependent part of the LILO delay. Depends upon the “mismatch” between input and output speed.
- MIMO measures the delay introduced only by switch itself.

For the n-cell Frame: n depends upon the workload

- $\text{LILO} = (3n+1)c$ ,  $\text{LILO}_0 = 3nc$ ,  $\text{MIMO} = 1c$

---

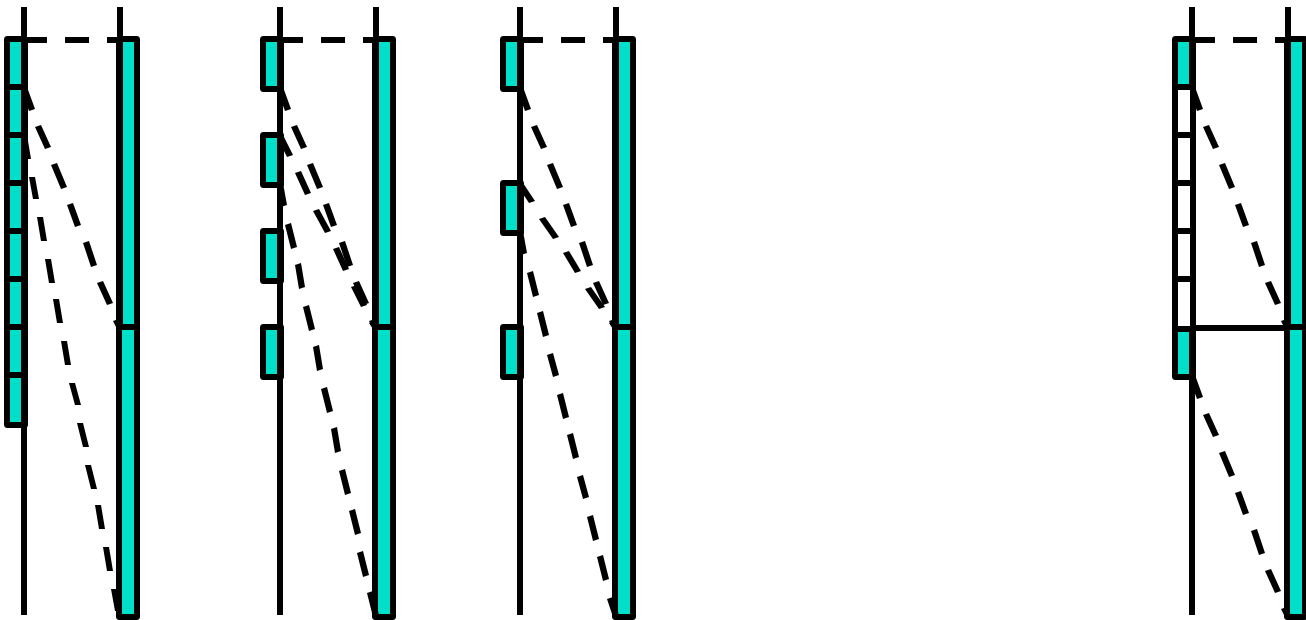
# Measurement Configuration



---

# Workload

Input Rate (155 Mbps) > Output Rate (25 Mbps)  
Gaps between the cells of the frame increased from 0 to 7 cells. Queueing up to 5-cell gap



---

# Measurement Results

Input 155Mbps, Output 25Mbps, 32-cell frame

LILO and FILO depend heavily from frame pattern

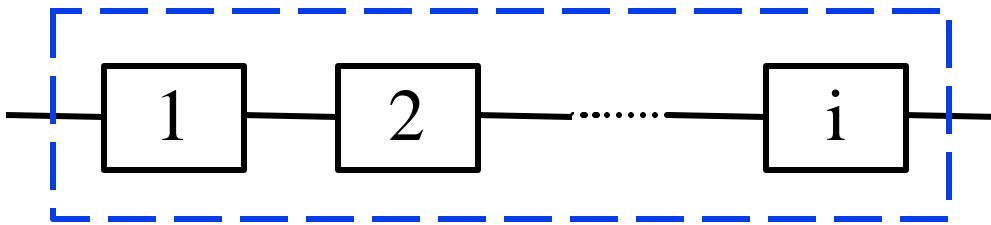
MIMO indicates the switch contribution in the delay

Test No.	Frame Pattern	LILO <sub>0</sub>	LILO	FILO	MIMO
1	No gap	351.71	385.01	563.3	33.3
2	1-cell gaps	263.98	295.78	561.8	31.8
3	2-cell gaps	176.25	209.05	562.8	32.8
4	3-cell gaps	88.52	119.82	561.3	31.3

All times are in microseconds

---

# MIMO Latency of a Path



For each switch or wire:

- $MIMO_i = LILO_i - LILO_{0i}$

Similarly for the network path:

- $MIMO_{\Sigma} = LILO_{\Sigma} - LILO_{0\Sigma}$

Since:  $LILO_{\Sigma} = \Sigma LILO_i$

- $MIMO_{\Sigma} = \Sigma MIMO_i + \Sigma LILO_{0i} - LILO_{0\Sigma}$

---

# Delay Components in a path

$$MIMO_{\Sigma} = \Sigma MIMO_i + \Sigma LILO_{0i} - LILO_{0\Sigma}$$

$MIMO_i$  component delay introduced by switch  $i$

$LILO_{0i}$  workload-dependent component delay

introduced the mismatch of the input-output speeds

the  $i$ th component.  $LILO_{0i}$  can be computed from

input/output speed of the  $i$ th component

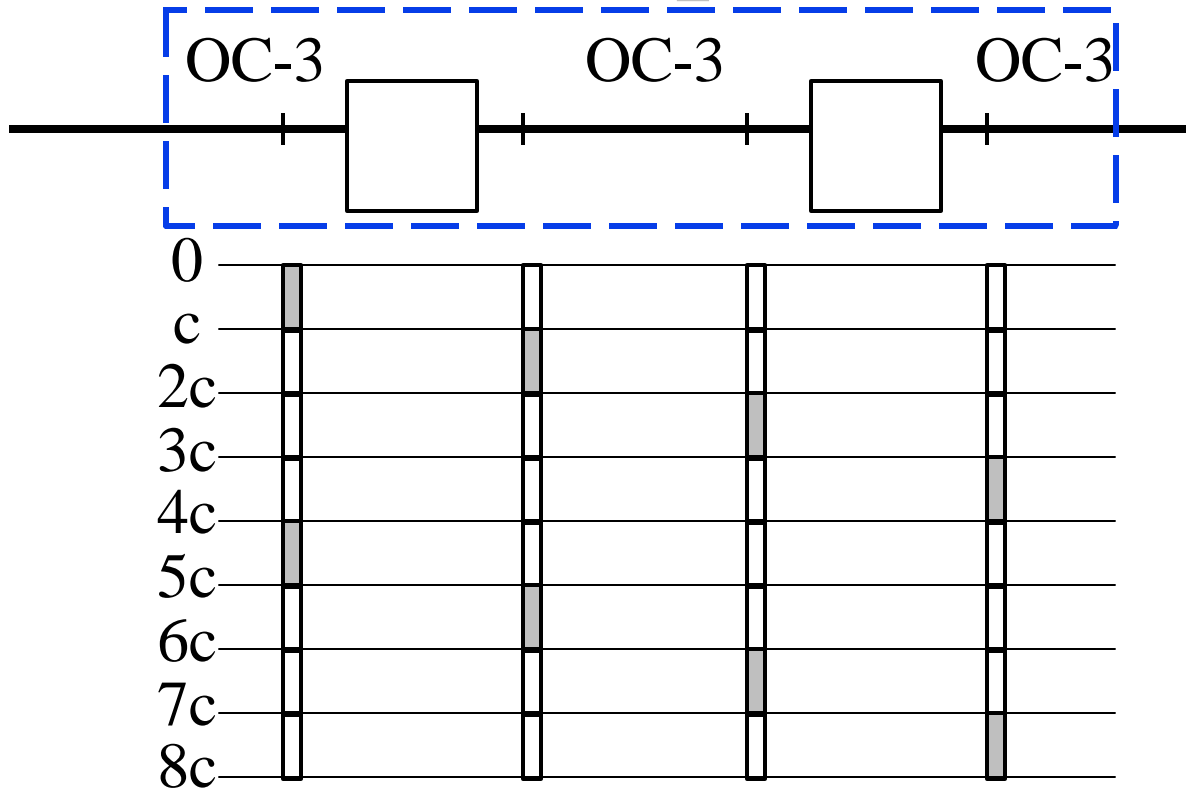
$LILO_{0\Sigma}$  workload-dependent delay that would have

been introduced if the path were to be replaced by an

ideal switch.  $LILO_{0\Sigma}$  can be computed from the

input/output speed of the entire path.

# Example 1

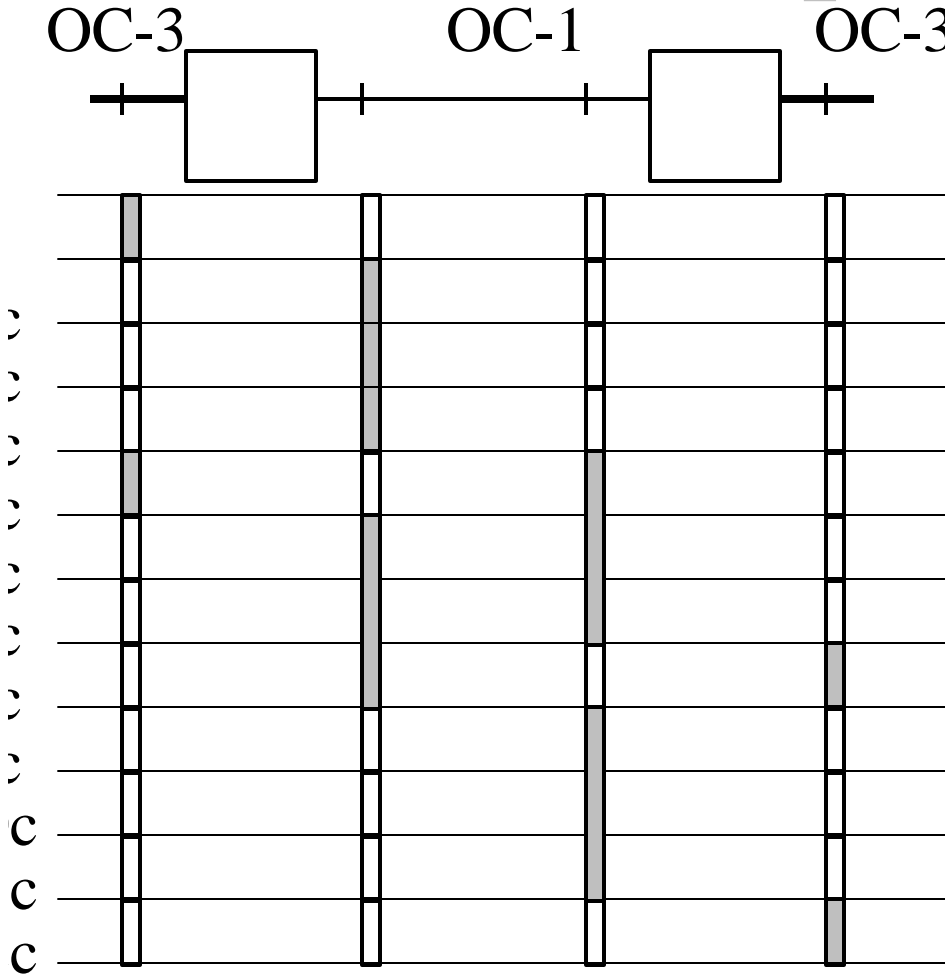


For each component: Input = Output  $\Rightarrow$   $LILO_{0i} = 0$

For the path: Input = Output  $\Rightarrow$   $LILO_{0\Sigma} = 0$

$$MIMO_{\Sigma} = \sum MIMO_i + \sum LILO_{0i} - LILO_{0\Sigma} = c + c + c =$$

# Example 2



□ Middle link OC-

○  $MIMO_1 = c$

○  $MIMO_2 = 3c$

○  $MIMO_3 = c$

□  $LILO_{01} = 2c$

□  $LILO_{02} = 0$

□  $LILO_{03} = 0$

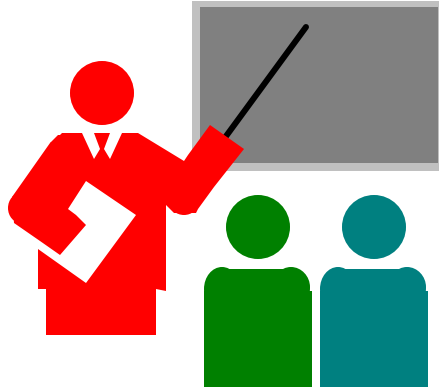
□  $LILO_{0\Sigma} = 0$

$$MIMO_{\Sigma} = \sum MIMO_i + \sum LILO_{0i} - LILO_{0\Sigma}$$

$$= (c+3c+c) + (2c+0+0) - 0 = 7c$$

---

# Summary



FIFO and LIFO are significantly affected by the workload

FIFO is meaningless if large gaps in the frames

LIFO is meaningless if large number of back-to-back frames

MIMO provides system latency.

MIMO can be aggregated.